# Peak-Hour Road Congestion Pricing: 

# Experimental Evidence and Equilibrium Implications * 

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#### Abstract

Developing country megacities suffer from severe road traffic congestion, yet the level of congestion is not a direct measure of equilibrium inefficiency. I study the peak-hour traffic congestion equilibrium in Bangalore. To measure travel preferences, I use a model of departure time choice to design a field experiment with congestion pricing policies and implement it using precise GPS data. Commuter responses in the experiment reveal moderate schedule inflexibility and a high value of time. I then show that in Bangalore, traffic density has a moderate and linear impact on travel delay. My policy simulations with endogenous congestion indicate that optimal congestion charges would lead to a small reduction in travel times, and small commuter welfare gains. This result is driven by the shape of the congestion externality. Overall, these results suggest limited commuter welfare benefits from peak-spreading traffic policies in cities like Bangalore.


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## 1 Introduction

Traffic congestion is a significant and pervasive problem in large cities, especially in developing countries, where the urban population and private vehicle ownership are growing rapidly. For example, the fastest large city in India is slower than the slowest large city in the US (Akbar et al. 2021). Long and unreliable travel times reduce the agglomeration benefits of large cities, whether for accessing jobs, markets, services or amenities.

Commuters who drive in congested conditions impose externalities by increasing travel times for the other commuters on the road. Since congestion is higher during rush hour, peak-hour traffic jams may be particularly inefficient. Reflecting this concern, several urban road traffic policies focus on reducing peak-hour congestion, either through pricing or quantity restrictions 1

However, while congestion pricing is the textbook policy response to traffic externalities, its quantitative relevance to traffic congestion in developing countries is an empirical question. This is because high peak-time congestion levels do not automatically imply a significantly inefficient allocation of traffic.

In this paper, I study the impact of peak-hour congestion pricing on driver behavior and on the peak-hour traffic congestion equilibrium in Bangalore, India. I measure the following demand and supply fundamentals that I will hold fixed in counterfactuals. First, I estimate commuter travel preferences, including desired arrival times, using precise data on urban travel behavior and experimental price variation. Second, I estimate the causal effect of traffic density on travel speed, thereby characterizing the road traffic externality in Bangalore given the current road network, vehicle composition and driving styles.

I set up an equilibrium model of peak-hour congestion, adapting the classic trip scheduling model Vickrey, 1969). Commuters choose an optimal trip departure time based on the distribution of travel times for different departure times. For model estimation, I also incorporate a dynamic choice between two routes that differ in travel time profiles. Commuters have rich heterogeneity given by an unobserved distribution of ideal arrival times and logit or nested logit shocks. The key preference parameters are the value of travel time (VOTT), and the schedule costs of arriving early or late, relative to the ideal arrival time. In the benchmark equilibrium model, the profile of congestion on the unique route is determined endogenously by aggregate departure rates. I also analyze an equilibrium model extension with two routes that have different externalities (as in Walters 1961, and another extension with an extensive margin decision.

I use a version of this model to design a field experiment with congestion charge policies to estimate the preference parameters. I implement the experiment within a sample of 497 commuters in Bangalore. I collected detailed travel behavior data using a smartphone app that passively logged GPS location data from study participants. The two congestion pricing policies induce exogenous cost variation along the departure time and travel time dimensions. The "peak-hour" pricing policy gives some commuters marginal incentives to change their departure times. Under the "route" pricing

[^1]policy, commuters pay a flat fee for driving through a circular area located along their usual route. The area is chosen individually for each commuter to induce a choice between a quick, expensive route and a longer free detour route. I implement the experiment using a smartphone app and a pre-paid account. Intuitively, commuter departure time and route choices with and without these two pricing policies help identify the schedule cost parameters and VOTT.

Commuters respond to the two treatments by changing departure times and routes to avoid charges. Under "peak-hour" charges, in the morning before the peak-hour, commuters left around 3-4 minutes earlier on average, with an imprecise response after the peak-hour. My results for the evening peak-hour are less precise, but consistent with commuters leaving later after the peak. I find no impact on the number of trips. Under "route" charges, participants use the detour (free) route 27 percentage points more often. Higher detour route usage persists after charges end, including among commuters who used a detour route before the experiment.

I use moments that exploit the experimental price variation to estimate the travel demand model of departure time and route choice for the morning commute.

The estimated value of travel time is 609 INR per hour (9.5 USD at market exchange rates or 29.5 USD PPP in 2017). This is significantly larger than the average self-reported hourly wage in this sample, indicating that commuters significantly dislike driving in Bangalore. VOTT is identified separately from a route switching cost included in the dynamic route choice model. Another reason for large estimated VOTT is that my results are relative to time differences based on Google Maps, while commuters in this sample overestimate differences in travel times.

The estimated schedule costs of early and late arrival are 552 INR per hour and 344 INR per hour, showing that commuters are moderately schedule inflexible. The cost of early arrival is higher than previous estimates as a fraction of VOTT, while the cost of late arrival is smaller (Small, 1982 ). Schedule flexibility allows commuters to protect themselves from high peak-hour congestion by changing their departure times. However, the effect of flexibility on the deadweight loss of congestion is ex ante unclear, because flexibility affects both the equilibrium and the social optimum.

I next measure the road traffic externality. To measure traffic density, I use around 120,000 GPS trips collected using the smartphone app over six months in 2017. I use Google Maps data to measure instantaneous travel delay (inverse speed). To identify the causal impact of traffic density on travel delay, I use the large variation in traffic delay at different times of the day, including between peak- and off-peak-hours, similar to Akbar and Duranton (2017).

Citywide traffic density has a moderate and linear impact on travel delay. The linear relationship is robust for all calendar dates and when zooming in to major arteries. I find no evidence of convexity for high levels of traffic. Quantitatively, a 7 km long peak-hour trip increases total driving time in Bangalore by approximately 15 minutes. I discuss additional robustness results and possible omitted variables. The citywide relationship that I estimate is biased if commuters substitute to higherexternality roads during the peak-hour (Walters, 1961). I use Google Maps route data to show that this effect is small for Bangalore commuters.

In the final part of the paper, I simulate an equilibrium model where commuters decide when to travel, and congestion is determined endogenously. Commuters are endowed with the preferences I estimate from my field experiment, and congestion is determined by the road network technology I
estimate from GPS data. In the benchmark model, commuters have a single route. I compare the unpriced Nash equilibrium to the social optimum implemented with equilibrium optimal departure time by trip length Pigouvian congestion charges, assuming zero policy implementation costs and lump-sum revenue redistribution.

Through the lens of the model, optimal departure time charges have a small effect on commuter welfare. Under the social optimum, peak congestion is lower and the average trip duration goes from 37.4 to 34.9 minutes on average, a $17.6 \%$ reduction in average travel time above free-flow. Commuter welfare - which also includes schedule costs-increases by 9.4 INR ( 46 US cents PPP) or $2.3 \%$. These low welfare gains are robust to varying commuter preferences and adding preference heterogeneity.

These results depend strongly on the shape of the externality. Welfare gains would be significantly higher with a more convex relationship between traffic volume and travel times. Since the shape of the road traffic externality may be different in other cities, this result suggests that measuring city-wide road traffic externalities is of first-order importance. The welfare gain is somewhat higher in an equilibrium model where commuters choose between two routes with different externalities (Walters, 1961).

My simulations ignore longer-term margins of adjustment, such as commuter and firm location choices (Tsivanidis, 2019 Herzog, 2022). Congestion pricing can have ambiguous effects on welfare in such contexts Brinkman, 2016). To provide some insight into other margins of behavior, I run simulations where commuters can adjust along the extensive margin, a catch-all for using travel modes that have negligible externalities (such as public transportation) and for canceling trips. Welfare gains remain low for reasonable values of the elasticity of trips with respect to total trip cost.

## 2 Related Literature

This paper builds on an extensive theoretical literature analyzing optimal and second-best pricing with peak-hour road traffic congestion (Vickrey, 1969, Small, 1982; Arnott et al. 1993; Noland and Small, 1995, Hall, 2018, 2020). My model builds on the canonical trip scheduling model, adding and estimating additional sources of heterogeneity to better match individual travel behavior data.

The dynamic model of traffic congestion I use here is related to the hydrodynamic or kinematic model with the assumption of instantaneous propagation of traffic density in the entire city (Mahmassani and Herman, 1984; Small et al. 2007). Other canonical models of peak-hour congestion are the bottleneck model with fixed capacity (Vickrey, 1969 Arnott et al. 1993), and models without propagation (Chu, 1995 Henderson, 1974). To estimate the impact of citywide traffic density on travel delay in Bangalore, I use predictable daytime variation in traffic density Akbar and Duranton, 2017. Hughes and Kaffine, 2018, Anderson and Davis, 2020).

The approach in this paper to design an experiment based on the model brings together two previous literatures. First, some papers use discrete choice models to estimate the value of time, of reliability, or of urgency from real-world driver decisions to use a faster tolled lane (Small et al. 2005 Bento et al. 2020). A separate group of papers analyzes reduced form impacts of road pricing
experiments (Tillema et al. 2013 Martin and Thornton, 2017). In this paper, the randomized experiment is designed to transparently recover the key commuter preference parameters in the model, the value of travel time and scheduling preferences.

A related empirical literature documents the impact of real-world traffic policies on traffic volumes, travel times and air pollution, either for the aggregate impact of congestion pricing policies in London, Stockholm and Milan (TfL, 2006; Prud'homme and Bocarejo, 2005, Raux, 2005 , Gibson and Carnovale, 2015 Karlström and Franklin 2009), or for non-price, vehicle quantity restrictions in developing countries (Davis, 2008; Kreindler, 2016; Hanna et al. 2017, Gu et al., 2017).

Akbar and Duranton (2017) reach a similar conclusion of low deadweight loss due to traffic congestion for Bogotá, Colombia, using a representative household travel survey and Google Maps travel time data to estimate the demand for trips and supply of travel by time of day. My paper's key contributions are to explicitly incorporate substitution between different times of the day in the equilibrium model, and using an experiment to estimate demand.

## 3 Traffic Congestion and Travel Behavior in Bangalore, India

Similar to other large cities in developing countries, Bangalore's fast-growing population and economy put stress on its transportation network. Akbar et al. (2021) rank Bangalore as the most highly congested city in India.

Figure 1 shows travel delay based on travel times collected using the Google Maps API. On average between 7 am and 10 pm on weekdays and across all routes, it takes 3.6 minutes to advance one kilometer ( 10.3 miles per hour). This is extremely slow, broadly in line with speeds in other heavily congested large cities in developing countries, such as downtown Jakarta, Indonesia (Hanna et al., 2017) and Delhi (Kreindler, 2016).

Figure 1 also shows strong predictable within day variation in traffic congestion. Between 7 am and 9 am , travel delay increases by 1.38 minutes per kilometer. A trip that would take 40 minutes starting at 7 am would take more than an hour starting at 9 am . Similarly large changes in average travel delay occur around the evening peak. Most of the day to day variation in traffic in Bangalore is explained by route-by-departure time cells.

These patterns suggest that commuters exert high externalities during the peak-hour, and that a more efficient allocation would involve some of them leaving earlier or later. Individual-level travel behavior data from GPS data (discussed in section 5.1) is consistent with high schedule flexibility. Most commuters vary their departure times significantly from day to day. For the median person, the standard deviation of the departure time for the first trip of the day from home to work is 29 minutes, which implies a $95 \%$ probability interval of almost two hours (Table A1 panel C). However, this daily variation does not automatically imply that commuters are schedule flexible. It is possible that desired travel times change from day to day (based on changes in work or other constraints) and commuters are inflexible around those times on any particular day. The model and experiment will help clarify and quantify these issues.

Separately, the peak-hour congestion profile is not directly informative about the magnitude of the traffic externality. Quantifying the externality requires measuring the underlying variation in
traffic density, which I do in section 8

## 4 Theoretical Framework

In this section, I set up an equilibrium model of peak-hour traffic congestion. In the model, a commuter chooses their optimal departure time based on the profile of traffic congestion and ideal arrival time. To study experimental variation in travel time, I extend the model to include route choice in a dynamic setting. I discuss how the elasticities identified in partial-equilibrium pricing experiments relate to the key travel demand model parameters. On the supply side, the congestion profile is endogenous, given by a dynamic model where instantaneous speed depends on traffic density.

### 4.1 Travel Demand: Departure Time Choice

An atomistic commuter $i$ decides when to travel from home to work on day $t$. The decision to make a trip is inelastic. (I add an extensive margin decision in section 9 )

To begin, consider the case with a single route. Departure time $h$ takes discrete values, for example every minute. Utility at departure time $h$ depends on realized travel time $T$ and ideal arrival time $h^{A}$ as

$$
\begin{equation*}
v\left(h, T, h^{A}\right)=-\alpha T-\beta_{E}\left|h+T-h^{A}\right|_{-}-\beta_{L}\left|h+T-h^{A}\right|_{+} \tag{1}
\end{equation*}
$$

Travel time cost is linear and $\alpha$ measures the marginal value of travel time (VOTT). The second and third terms are the canonical way to measure scheduling preferences over arrival time $h+T$ (Arnott et al., 1993). Schedule heterogeneity is defined by an ideal arrival time $h^{A}$, and schedule costs by constant per-unit of time costs of arriving early $\beta_{E}$ and of arriving late $\beta_{L}{ }^{2}$

Travel time $T_{i t}(h) \sim \mathcal{T}_{i}(h)$ is random and realized after departure, drawn i.i.d. over days $t$. I assume that the researcher observes the distributions $\mathcal{T}_{i}(h)$. For any travel time distribution $\mathcal{T}$, I denote expected utility

$$
\begin{equation*}
\mathrm{E} v\left(h, \mathcal{T}, h^{A}\right)=\mathrm{E}_{T \sim \mathcal{T}} v\left(h, T, h^{A}\right) \tag{2}
\end{equation*}
$$

This model captures the main forces that determine departure time decisions within the peakhour equilibrium, and it makes several parametric assumptions. Travel time costs are linear, and schedule costs are piece-wise linear. However, uncertainty in travel time smooths out the profile of schedule costs, and makes it more difficult to arrive close to the ideal arrival time. This implicitly generates a value of travel time reliability. In the benchmark model, the parameters $\alpha, \beta_{E}, \beta_{L}$ are the same for all commuters. I later estimate a model where these parameters scale with income.

Each morning, the commuter observes the ideal arrival time $h_{i t}^{A}$, idiosyncratic shocks $\left(\varepsilon_{i t}(h)\right)$, and monetary charges $p_{i t}(h)$, and chooses departure time to maximize expected utility,

$$
\begin{equation*}
u_{i t}\left(h, h_{i t}^{A}\right)=\operatorname{Ev}\left(h, \mathcal{T}_{i}(h), h_{i t}^{A}\right)-p_{i t}(h)+\varepsilon_{i t}(h) . \tag{3}
\end{equation*}
$$

[^2]The idiosyncratic shocks $\varepsilon_{i t}(h)$ are distributed according to a type-1 extreme value distribution with scale $\sigma^{D T}$. This leads to multinomial logit choice probabilities conditional on $h_{i t}^{A}$.

The ideal arrival time is a second source of individual heterogeneity in the model. As explained below, this allows for more flexible substitution patterns between departure times. The ideal arrival time $h_{i t}^{A}$ is drawn i.i.d. over days $t$ from an individual-specific distribution over a discrete grid, with probability density function $f_{i}^{A}$. The researcher does not observe $f_{i}^{A}$. This distribution is not affected by pricing experiments, and I hold it fixed in counterfactuals. The distribution of ideal arrival times is individual-specific to help account for the variation of departure times both across and within commuters in the data (Table A1).

Model Identification. The goal of demand estimation in this setting is to separately identify the value of travel time $(\alpha)$, schedule costs (parameters $\beta_{E}$ and $\beta_{L}$ ), and schedule heterogeneity (ideal arrival times distributions $f_{i}^{A}$ ). Assume temporarily that the VOTT parameter $\alpha$ is known.

Using only observational data on departure times, it is challenging to tease apart schedule costs ( $\beta_{E}$ and $\beta_{L}$ ) from arrival time heterogeneity $\left(f_{i}^{A}\right)$. However, these parameters can be separately identified when there is data on how commuters respond to pricing based on departure times. I prove these two model identification statements formally in a simplified model that preserves the key elements of this setting (Appendix A.1).

The key issue is that the same observed distribution of departure times may be consistent with a concentrated ideal arrival time distribution $f_{i}^{A}$ and low schedule costs $\beta_{E}$ and $\beta_{L}$ (or high $\sigma^{D T}$ ), or with higher variance $f_{i}^{A}$ and steep $\beta_{E}$ and $\beta_{L}$ (or low $\sigma^{D T}$ ).

However, these scenarios have different implications for the cross-price elasticity of departure time $h^{\prime}$ with respect to the price of departure time $h$. When $h_{i t}^{A}$ is a constant, we get the logit model, which predicts that pricing at $h$ leads to substitution toward all other departure times $h^{\prime}$ in proportion to observed baseline shares. Meanwhile, when the distribution of $h_{i t}^{A}$ has high variance and $\beta_{E}$ and $\beta_{L}$ are consequently steep, the response to pricing at $h$ will be highly local, decreasing quickly in $\left|h-h^{\prime}\right|$.

Emergency or ambulance trips illustrate the idea of a wide distribution of random ideal arrival times coupled with inflexibility in schedule costs around those times. Commuter responses to peak-hour departure time pricing experiments generate useful variation because they depend on a combination of cross-price elasticities.

### 4.2 Travel Demand: Dynamic Route Choice

To introduce random variation in travel time cost, in the second experimental treatment, participants are charged for using their typical commute route, giving them the option to take (longer) detour routes to avoid charges.

To analyze these choices, I extend the departure time model to include route choice. The dynamic model features two routes that differ in travel time profiles. Agents face a route switching cost. These features are motivated by two key experimental results that I preview here: route charges have persistent effects after charges end, including among commuters who used a detour route at
baseline.
Time is discrete, with discount factor $\delta$. Route $r=0$ is the shorter, direct route from home-to-work, and $r=1$ is the detour route. The within period expected utility is defined similar to (3),

$$
\begin{equation*}
u_{i t}\left(h, r, h_{i t}^{A}, r_{i t-1}\right)=\mathrm{E} v\left(h, \mathcal{T}_{i}(h, r), h_{i t}^{A}\right)-p_{i t}(h, r)-\gamma \mathbf{1}\left(r \neq r_{i t-1}\right)+\varepsilon_{i t}(h, r) \tag{4}
\end{equation*}
$$

The $E v$ term captures travel time and schedule costs, after taking expectations over route-specific travel time $T_{i t}(h, r) \sim \mathcal{T}_{i}(h, r)$. Charges $p_{i t}(h, r)$ may now depend on route. $\gamma \geq 0$ is a symmetric cost that applies if the commuter switches routes. $\varepsilon_{i t}(h, r)$ follows an extreme value distribution with correlation within each route, with scale parameters $\sigma^{D T}$ and $\sigma^{R}$ for within- and across-route choice. Route-level nesting captures idiosyncratic factors such as the need to make a quick stop along one of the routes. The ideal arrival time $h_{i t}^{A}$ is distributed as in the model with a single route.

Within-period timing is unchanged. At the start of each period, the commuter observes the ideal arrival time $h_{i t}^{A}$ and shocks $\left(\varepsilon_{i t}(h, r)\right)_{h, r}$, and then chooses a route and departure time. The value function at the start of period $t$, before observing $h_{i t}^{A}$ and the logit shocks, is:

$$
\begin{equation*}
V_{i t}\left(r_{i t-1}\right)=\mathrm{E}_{h_{i t}^{A}} \mathrm{E}_{\varepsilon} \max _{h, r}\left(u_{i t}\left(h, r, h_{i t}^{A}, r_{i t-1}\right)+\delta V_{i t+1}(r)\right) \tag{5}
\end{equation*}
$$

The model has two possible states, defined by route choice in the previous period, and rich within-period heterogeneity given by the nested logit and the ideal departure time distributions. In steady state, $V_{i t}(r)=V_{i t-1}(r)$ and we can solve 5 by iteration. During the experiment, $V_{i t}$ also depends on current and anticipated departure time and route charges. This model nests the single-route departure time choice model conditional on route $r$ (Appendix A.4.1).

To shed light on how the value of travel time is identified, I analyze a simplified model that abstracts from departure time choice and assumes a constant within-period utility difference between the two routes. I later show that estimating this model yields very similar parameters. The utility function is

$$
u_{i t}\left(r, r_{t-1}\right)=-\alpha T_{i}(r)-p_{i t}(r)-\gamma \mathbf{1}\left(r \neq r_{t-1}\right)+\varepsilon_{i t}(r)
$$

where $T_{i}(0)<T_{i}(1)$ denote expected travel times for the two routes, and $\varepsilon_{i t}(r)$ is extreme value type-1 distributed. The value function satisfies

$$
V_{i t}\left(r_{i t-1}\right)=\mathrm{E}_{\varepsilon} \max _{r} u_{i t}\left(r, r_{i t-1}\right)+\delta V_{i t+1}(r)
$$

This model has three key parameters: VOTT $\alpha$, switching cost $\gamma$, and logit scale $\sigma^{R}$. This model is identified based on data on detour route choice probabilities in three situations: in steady state, with a route charge, and after a temporary route charge was lifted (Appendix A.2).

### 4.3 Closing the Model: Road Technology and Equilibrium

The key technological constraint inherent to road travel is that traffic density lowers speed. To describe how a profile of trip departure time choices determines a profile of travel delays, I set up a dynamic model with instantaneous citywide density propagation similar to Mahmassani and Herman
(1984). In the benchmark model, I focus on a single route with endogenous congestion. In section 9 I extend this to an equilibrium model with two routes with different externalities, similar to the Pigou-Knight model (Walters, 1961).

The city has a mass of atomistic commuters with trips of different lengths. A profile of departure time choices is defined by $Q=(q(h, K))_{h, K}$, where $q(h, K)$ is the mass of commuters with trip length $K$ who leave at $h$. At any time $h^{\prime}$, let $d\left(h^{\prime}\right)$ denote traffic density, the endogenous mass of ongoing trips, which I assume is homogenous in the entire city. All trips advance with the same instantaneous travel delay $x\left(h^{\prime}\right)$. Travel delay (inverse speed) is a function of density, $x\left(h^{\prime}\right)=$ $X\left(d\left(h^{\prime}\right)\right)$, and I assume it is bounded from above. The distance traveled between times $h$ and $h^{\prime}$ is $\int_{h}^{h^{\prime}} x\left(h^{\prime \prime}\right)^{-1} d h^{\prime \prime}=S\left(h^{\prime}\right)-S(h)$.

Density $d\left(h^{\prime}\right)$ is described by a differential equation,

$$
\begin{equation*}
\frac{d}{d h^{\prime}} d\left(h^{\prime}\right)=\underbrace{\int_{K} \pi\left(h^{\prime}, K\right) d K}_{\text {departures }}-\underbrace{\int_{K} \pi\left(H\left(h^{\prime}, K\right), K\right) d K}_{\text {arrivals }}, \tag{6}
\end{equation*}
$$

where $H\left(h^{\prime}, K\right)$ is the departure time for trips of length $K$ that end at $h^{\prime}$, defined by $S\left(h^{\prime}\right)-$ $S\left(H\left(h^{\prime}, K\right)\right)=K$. Thus, the profile of departures $Q$ uniquely determines travel times $\operatorname{ET}(h, K ; Q)$.

Commuters also face idiosyncratic travel time uncertainty. On day $t$, for commuter $i$ with trip length $K_{i}$, leaving at $h$, travel time is a random variable distributed according to $\psi_{i h t} \mathrm{ET}$ where $\mathrm{E} T=\mathrm{E} T\left(h, K_{i} ; Q_{t}\right)$ and $\psi_{i h t} \sim \Psi(\mathrm{E} T)$ for a family of distributions $\Psi(\cdot)$. Travel time draws are independent over $t$ but may be correlated across commuters and departure times. I later assume that $\Psi(\mathrm{E} T)$ is a log-normal distribution that I estimate from Google Maps data. This model for uncertainty is an approximation for a model where shocks to instantaneous speed propagate to travel times through equation (6).

This model has two forces for traffic congestion externalities. First, density has a direct effect on speed. Second, lower speeds decrease trip completion rates and hence increase density later on. The magnitude of the externality depends on the shape of the relationship $X(d)$ between density and travel delay, which I estimate for Bangalore in section 8

Equilibrium. An equilibrium of the single-route model is defined by two types of endogenous objects, the unconditional probability distributions over departure times $\left(\pi_{i}(h)\right)_{h}$ for each commuter $i$, and the citywide instantaneous travel delay profile $(x(h))_{h}$. The model primitives are commuter preference parameters, including their distributions of ideal arrival times $f_{i}^{A}$, the road technology $X$, and the family of travel time uncertainty distributions $\Psi(\cdot)$.

In equilibrium, the profile $x(h)$ uniquely determines expected travel times for any departure time and trip length. This profile is endogenous, determined by the commuter departure time choices and the road technology, based on (6). Commuter $i$ 's choices are optimal given their randomly drawn ideal departure time and the travel time profile specific to $i$ 's trip length, according to (3).

I compute the equilibrium using an iterative procedure (section 9). While a formal characterization of equilibrium uniqueness is beyond the scope of this paper, in these numerical simulations, and for a range of starting conditions, I find a unique equilibrium.

The social optimum is implemented as a Nash equilibrium with Pigouvian charges $p(h, K)$ equal to the marginal social cost imposed by a commuter with trip length $K$ who travels at time $h$. I use the terms "deadweight loss of congestion" and "welfare gains from optimal congestion pricing" interchangeably to refer to the difference in commuter welfare (average expected utility) between the social optimum and the unpriced Nash equilibrium.

The goal of the empirical part of this paper is to estimate the demand parameters and the road technology. The patial equilibrium experiment identifies travel preferences holding the citywide travel time profile fixed. Equilibrium responses to a citywide congestion pricing policy would also generate aggregate changes in the travel time profile. The simulations in section 9 explicitly incorporate this feedback.

## 5 Data Sources and Study Sample

The data backbone of the paper is a set of driving trips with precise GPS coordinates, collected using a newly developed smartphone app. This data was used both for measuring detailed driving behavior and for implementing the congestion charge policies in the experiment.

### 5.1 GPS Trip-level Data from Smartphone App and Other Data

Travel behavior data was collected using a smartphone app that works in the background of a GPSenabled Android smartphone and passively collects phone location data, without requiring any user input.

The raw GPS data for each user-day was automatically cleaned and classified into trips, locations, and missing-data segments. Consecutive trips with short stops of less than 15 minutes between them are linked together. ( $89 \%$ of trips in the sample have no stops.) During the experiment, I used this algorithm to compute congestion charges.

Measuring travel behavior automatically using a smartphone-based app has several advantages over surveys. Self-reported behavior is affected by recall bias, rounding of departure times and trip duration, and tends to underestimate within-person temporal and route variation (Zhao et al. 2015).

The app sometimes did not collect GPS data, for either technical or human factors. The analysis sample is restricted to days and trips labeled as high-quality. During the experiment, around $75 \%$ of days and $64 \%$ of trips are good quality. See section SM. 2 for details.

I identify home and common, recurring daytime destinations at the commuter level (such as a work or school) using a clustering algorithm to group locations into groups, followed by manual review of the location groups most frequently visited. Next, I compute the fraction of distance traveled between "home" and "work," as well as the fraction of days present at work. Using these two variables,

I classify participants into regular and variable commuters, based on identifying home and regular daytime (work, school) locations. I identify these common locations using a clustering algorithm applied to the set of all trip start and end locations, followed by manual review of the most frequently visited clusters. Around $75 \%$ of participants are regular commuters, and the median regular
commuter visits work on $91 \%$ of weekdays (Table A1. Panel B).
collected three types of Google Maps data on travel times that include information on traffic congestion. The first data set collected real-time travel time on 30 routes in the study area of South Bangalore, every 20 minutes throughout the day, for 207 days in 2017. I use this data to calibrate the distribution of travel times, and to measure the impact of traffic density on speeds. To measure choice sets, for each regular commuter, I collected data on typical travel times between home and work locations, at all departure times during the day. To measure the Pigou-Knight trade-off, I collected the typical travel time profiles for all routes between home and work.

### 5.2 Study Sample, Survey Data, and the Congestion Charge Platform

Study participants were recruited in a random sample of gas stations in South Bangalore. Surveyors approached private vehicle drivers (commuters) who were using a car, motorcycle or scooter, excluding professional drivers. Study participants who owned their vehicle, traveled regularly were eligible for the study. Respondents also had to own a GPS-enabled Android smartphone to participate, and $76 \%$ of otherwise eligible drivers did. Respondents were invited to install the study smartphone app and answer a short survey. Surveyors collected some data for all those approached: perceived age, gender, and vehicle information. Out of 16,911 persons approached, 2,299 installed the app, an estimated $27 \%$ of all eligible respondents (section SM.4.1).

After recruitment, the app collected baseline travel behavior data from study participants. I collected additional phone survey data from a random sub-sample of app users and all experiment participants, including travel time beliefs and hypothetical choice questions that mapped to the two main experiments (see section SM.4.2).

497 ( $22 \%$ of all app participants) were enrolled in the experiment on a rolling basis, based on app data quality. Surveyors met in person with each participant (including those in the control group) to explain the experiment (Figure SM2).

During the experiment, congestion charges were deducted from a pre-paid virtual account, and transferred by bank transfer at the end of each week. Participants were charged a fee for severely incomplete GPS data, and if they did not make any trips on a given weekday. The "no trip" fee was designed to dissuade incentive gaming by leaving the smartphone at home.

During the initial meeting, surveyors framed the account balance as the "respondent's money," and congestion charge as losses. During the experiment, charges were computed automatically and participants received daily account balance updates through SMS and app notifications. In addition, weekly phone calls reminded participants about their treatment group details. These features were designed to ensure salience of the congestion charges, which affects demand elasticities (Finkelstein, 2009).

## 6 Congestion Charge Policies: Design and Impact

### 6.1 Experimental Design

Departure Time Congestion Charges. Participants in this treatment were charged for each trip based on a per-km rate and the length of their trip. The rate followed a trapezoidal shape over a 3-hour interval, one in the morning and another in the evening (Figure SM2). The rate profile has one-hour increasing and decreasing ramps around a one-hour flat peak period. The position of the charged interval differed by at most $\pm 30$ minutes between commuters, and was designed to maximize the overlap between the ramp periods and typical departure times for that commuter, based on baseline data. This procedure was implemented for all commuters before randomization.

There were four sub-treatments: control, information, low rate, and high rate. Participants in the control group were monitored for 5 weeks, received regular updates about their data quality, and received a flat 300 INR payment per week for participation. Participants in the information group received daily messages about the trips they had completed the previous day, and information about how to reduce trip travel time by changing departure time. They also participated for 5 weeks. This treatment helps separate the impact of prices from other features of the intervention, including experimenter demand effects.

Charges lasted three weeks. The low and high rate groups had a maximum (peak) congestion rate of $12 \mathrm{INR} / \mathrm{Km}$ and $24 \mathrm{INR} / \mathrm{Km}$, respectively. They received daily messages about the trips they had completed the previous day, how much each was charged, and information about how to reduce trip charges by changing departure time.

Route Congestion Charges. Participants in this treatment were charged if they drove through a congestion area. The area was a disc with radius $250 \mathrm{~m}, 500 \mathrm{~m}$ or 1000 m positioned along a route used frequently by the participant during the pre- period. The area induced an alternate nonintersecting detour route, which was between 3 and 14 minutes longer than the original route, based on Google Maps travel time data. Study participants never had a stable destination inside the congestion area. This procedure was possible for 254 out of the 497 experiment participants; the remaining 243 were not included in the route treatment. During the meeting, surveyors carefully explained the area location, radius, boundaries, and one possible induced detour. This information was repeated in each daily reminder SMS. Surveyors explained that only routes that intersect the area will be charged, and that several detour routes may exist.

The route treatment did not include a pure control group. Participants were randomized between being treated in the first week in the experiment (early) or in the last week (late). The charge was in effect between 7 am and 9 pm , and applied at most once for the morning interval ( $7 \mathrm{am}-2 \mathrm{pm}$ ) and at most once for the evening interval ( $2 \mathrm{pm}-9 \mathrm{pm}$ ).

Sub-treatments were designed to identify the effect of price and detour time variation on choices. Low/high rate participants had a baseline charge of $80 / 160$ INR. Long/short detour participants had random variation in detour length (section SM.5. ${ }^{3}$

[^3]The randomization was stratified based on route treatment eligibility, vehicle type, and baseline daily travel length (Table A2). The route treatment timing (early/late), the low/high rate, and the long/short detour sub-treatments were cross-randomized, giving 8 equal-probability treatment cells. Participants received the departure time treatment for three consecutive weeks, either the first three or the last three, randomly chosen. When applicable, this was dictated by the timing of the route treatment. The route and departure time treatments never occurred at the same time. The four departure time sub-treatments and the eight route sub-treatments were cross-randomized within each stratum (section SM.6).

The different treatment groups are balanced along demographic and pre-period travel behavior variables (Table A4). The congestion charge treatments did not affect data quality (Table A5).

### 6.2 Reduced-Form Responses to Congestion Charges

I first discuss the representativeness of the experimental sample. The 497 experimental participants represent $6 \%$ of all eligible commuters approached by surveyors in gas stations (Table A3). Almost all commuters in this setting are men. Experiment participants appear 2 years younger and are slightly less likely to use a car. Among survey respondents, experiment participants report similar income, report traveling slightly more, and they have slightly higher stated values of time and stated schedule flexibility.

In the GPS data, at baseline, commuters make around 3 trips per day on average, each around 25 minutes and 6 km long (Table A1). Three quarters of the sample are regular commuters. Most commuters in this sample have variable departure times.

The Impact of Departure Time Charges. In principle, commuters may respond to charges by canceling trips with departure times during the charged period (extensive margin), as well as by rescheduling trips to departure times with lower charges (intensive margin).

Figure 2 provides a first look at the causal impact of congestion charges on the number of trips and on the distribution of trip departure times. It shows the difference-in-differences of the number of trips by departure time bin, during vs before the experiment and in the treatment group vs the control group. I pool the control and information sub-treatments, and the low- and high-rate sub-treatments.

In the morning, there is no reduction in the total number of trips, as the integral of the curve is non-negative. In the early morning, there is a strong shift in trips towards earlier departure times. In this interval, charges create a marginal incentive to leave earlier. Commuters in this interval leave around 4 minutes earlier on average due to the treatment (Table SM4. $4_{4}^{4}$ In the evening, the figure shows a decrease in the number of trips in the later part of the congestion charge ramp, consistent with a combination of extensive and intensive margin responses.

[^4]I run the following difference-in-differences specification:

$$
\begin{equation*}
y_{i t}=\gamma^{I} T_{i}^{I} \times \text { Post }_{t}+\gamma^{L} T_{i}^{L} \times \text { Post }_{t}+\gamma^{H} T_{i}^{H} \times \text { Post }_{t}+\mu_{t}+\alpha_{i}+\varepsilon_{i t} \tag{7}
\end{equation*}
$$

where $y_{i t}$ is an outcome of interest for commuter $i$ on day $t$, Post $_{t}$ is a dummy for the experimental period, $T_{i}^{I}, T_{i}^{L}$ and $T_{i}^{H}$ are dummies for the information, low rate and high rate departure time sub-treatments, $\alpha_{i}$ and $\mu_{t}$ are commuter and time fixed effects. The coefficients of interest, $\gamma^{I}, \gamma^{L}$ and $\gamma^{H}$, respectively measure the impact of information, low rates and high rates relative to control, during the experiment relative to the period before. For higher precision, in some analysis I pool low rate or high rate sub-treatments together, as well as the control and information sub-treatments.

The sample is all non-holiday weekdays when the respondent does not travel outside Bangalore. During the experiment, I include the three weeks when charges are in effect, with comparable timing in the control and information groups.

Table 1 shows results on daily outcomes. The first three columns show impacts on total daily "trip hypothetical rate." This outcome is the sum over all trips in the day of the commuter's own congestion rate profile (defined for all participants irrespective of treatment group) and using a normalized peak rate of 100 . This outcome is computed uniformly across commuters and across time, and it is a summary statistic for whether the commuter's travel behavior is associated with high charges. It combines both intensive and extensive margin responses. The last three columns report results on the total number of trips.

In the high rate sub-treatment, the total daily hypothetical rate drops from a base of 96 to around 84 , a $13 \%$ decrease. The low rate sub-treatment coefficient is also negative but smaller in magnitude and not significant. When disaggregating by morning and evening in the second and third columns, results are similar but less precise. The information group does not have a statistically significant effect. The daily SMS and app reminders did not, by themselves, affect departure time travel behavior as summarized by hypothetical rates. Among regular commuters, charges fall more early relative to late in the morning, and late relative to early in the evening (Table A6).

Departure time charges have a small and often insignificant effect on the total number of trips. The point estimate on high rate in the fourth column implies a $2 \%$ decrease in the number of trips, and the point estimate on Charges in the same column implies a $4 \%$ decrease. However, there is a marginally significant decrease in the evening of $7 \%$. This result mirrors the findings from Figure $22^{5}$ Treatment effects do not vary statistically significantly over time during the experiment (Table SM2.

The Impact of Route Charges. Figure 3 shows the average detour usage rate among home-towork trips by route treatment group over time. Before the experiment, the detour route usage is between 8 and $12 \%$, and $39 \%$ of commuters use a detour route at least once at baseline.

When charges first go into effect, the detour usage rate jumps to $40 \%$ for the participants who are charged in week 1, relative to $12 \%$ for those who expect that they will receive charges in week 4 . When the latter group experiences charges, their detour route usage rate goes up to around $35 \%$.

[^5]Charges have a persistent effect on route choice. Focusing on the early group, the detour rate is around $20 \%$ in weeks 2,3 and 4 , after route charges are no longer applicable. This persistence is consistent with switching costs (i.e. habit) or a fixed cost of learning about the detour route (Larcom et al. 2017).

Commuters who used a detour route at least once at baseline also see persistence after charges end. I show this in Panel B of Table A7. The table shows the regression counterpart of Figure 3 (see also section A.3). This finding suggests that persistence is due to switching costs rather than due to learning about a new route, motivating the use of switching costs in the dynamic route choice model in section 4.2

Effects from randomly higher route charge amount and from randomly shorter detour duration point in the expected direction but are imprecise (Table A8). When I analyze all variation in detour duration, I find that the impact of charges and persistence are higher for commuters with shorter detours (Figure SM4). The main treatment effects do not vary statistically significantly over the five days during the experiment (Table SM2).

## 7 Travel Demand Estimation

I now use the data and the experimental variation to estimate the key parameters in the travel demand model. This will provide monetary measures of individual preferences over schedule inflexibility and the marginal value of travel time (VOTT).

### 7.1 Estimation Overview and Experimental Moments

The benchmark model for estimation is the dynamic route choice and departure time choice model from section 4.2. To explore robustness to model assumptions, I also estimate several simpler models, including varying how route choice is modeled, using calibrated VOTT, and abstracting from departure time choice.

I use the generalized method of moments (GMM), with moments chosen to leverage the experimental variation in costs of departure time and route choice (Appendix A.4.2.

The first set of moments measures how departure time "market shares" shift in response to peakhour pricing, as shown in Panel A of Figure A1. There is a moment for each 5-minute departure time bin in $[-2,+2]$ hours around the departure time charge profile midpoint ( 49 moments). For each commuter and each bin, I compute the average fraction of trips starting in that bin. For each bin, I then average this value across commuters, within four cells given by period (before or during the experiment) and treatment group (control or charges). Finally, I compute the difference-indifferences for each departure time bin $\left[^{6}\right.$

The second set of 10 moments measures detour route choice probabilities across time (before the experiment, and four weeks during the experiment) and treatment group (early and late route charges), corresponding to Figure 3

[^6]Intuitively, the departure time moments are informative about schedule costs and the departure time logit parameter, while the dynamic route choice moments help pin down VOTT, the switching cost, and the route logit parameter. I explore the mapping between data and estimated parameters formally in Section 7.4

### 7.2 Data, Travel Time Distributions, and Estimation Sample

I use two types of Google Maps data to construct choice sets. For average driving times $\mathrm{E} T_{i t}(h, r=0)$ and short route length $K_{i}$, for each study participant, I collected Google Maps predicted driving times on their home-to-work route at all departure times throughout the day. To calibrate travel time uncertainty, I use the real-time Google Maps data.

I assume that driving time follows a log-normal distribution around the measured Google Maps average driving time. Within route by departure time cells, driving time is approximately log-linearly distributed across the 145 weekdays in the data, with the standard deviation well explained by a quadratic in the average driving time (Figures SM6 and SM7).

For route treatment participants, the travel time profile on the detour route $(r=1)$ is proportional to short route travel time profile, with an individual-specific factor. I calibrate this factor using Google Maps the driving time at 9 AM for the quickest route that does not intersect the congestion area, which I obtained before the experiment. Note that travel time uncertainty is also higher on the detour route.

Commuters face known monetary charges $p_{i t}(h, r)$ exactly as in the experiment. The trip sample is all morning home-to-work trips. Out of 378 regular commuters, the estimation sample consists of 304 commuters who have at least one sample trip during the experiment for either the route treatment or the departure time treatment.

### 7.3 Solving the Model and Inverting Ideal Departure Time Distributions

Model Setup. The benchmark estimation model is described in section 4.2. To bring the model to the data, I assume that departure times take values every 5 minutes from -2.5 to +4 hours relative to the departure time charge profile midpoint. Ideal arrival times take values on an equally-sized grid between -2 to +4.5 hours relative to the same point. The time period in the dynamic route choice model is one week. This choice is motivated by computational considerations and the fact that in the data, $75 \%$ of the time, route choice is constant within week.

I estimate a fixed effect that enters the detour route utility ( $r=1$ ) in equation (4). The term $\eta_{\text {early }}$ is switched on for all commuters in the early route treatment, for all time periods. (Results without $\eta_{\text {early }}$ are similar.)

I normalize the nested logit parameters to be proportional to a commuter's pre-experiment short route length $K_{i}$. Commuter $i$ has $\sigma_{i}^{D T}=\frac{K_{i}}{\bar{K}} \sigma^{D T}$ and $\sigma_{i}^{R}=\frac{K_{i}}{\bar{K}} \sigma^{R}$ where $\bar{K}$ is average trip length in the sample. Since costs in the utility function scale approximately linearly with route length, this normalization prevents commuters who travel far from having mechanically more precise choices, as would be implied by constant $\sigma^{D T}$ and $\sigma^{R}$.

The discount factor is typically difficult to estimate in discrete choice models Abbring and Daljord 2020). In the benchmark model I calibrate $\delta=0.9$ and I later show robustness to different values and to estimating $\delta$.

The preference parameter vector to estimate is $\theta=\left(\alpha, \beta_{E}, \beta_{L}, \gamma, \sigma^{D T}, \sigma^{R}, \eta_{\text {early }}\right)$. $\alpha$ measures VOTT, $\beta_{E}$ and $\beta_{L}$ are early and late schedule costs, $\gamma$ is the route switching cost, $\sigma^{D T}$ and $\sigma^{R}$ are the logit parameters, and $\eta_{\text {early }}$ is the early group detour route fixed effect. For each commuter $i$, I will invert the probability distribution function of ideal arrival times, $f_{i}^{A}$.

Computing Choice Probabilities. Given a parameter vector $\theta$, solving the model consists of computing choice probabilities over departure times and routes, for each participant and for each time period before and during the experiment. I do this in two steps. I first compute choice probabilities taking the distribution of ideal arrival times as given, and then I invert this distribution from observed pre-experiment departure times (Appendix A.4.1).

To begin, assume that the distribution $f_{i}^{A}\left(h_{i t}^{A}\right)$ of ideal arrival times is known for commuter $i$. Conditional on an ideal arrival time $h_{i t}^{A}$, I derive a closed form expression for expected utility in equation (2) when travel time is log-normally distributed. This yields departure time probabilities conditional on route, $\pi_{i t}\left(h \mid h_{i t}^{A}, r, \theta\right)$. (Whenever applicable, this expression implicitly depends on pricing.) In particular, route switching costs $\mathbf{1}\left(r \neq r_{i t-1}\right)$ and future period valuations $\delta V_{i t+1}(r)$ drop out. For the 99 commuters who are not in the route experiment, I use the single route model, and hence these expressions fully describe choice probabilities. I also derive expected utility $\mathrm{E} u_{i t}\left(h \mid h_{i t}^{A}, r, \theta\right)$.

I find the steady state of the dynamic route choice model by iterating the Bellman equation (5) to find the two values $V_{i}(r=0 \mid \theta)$ and $V_{i}(r=1 \mid \theta)$. At each step, I integrate within-period heterogeneity given by ideal arrival times. For each commuter, I assume steady state per-period utilities before and after the experiment. I solve backward for utility for weeks during the experiment and propagate route and departure time choice probabilities forward starting with steady state probabilities before the experiment. This yields route choice and departure time probabilities for each commuter, integrated over the distribution of ideal arrival times.

Inverting the Ideal Departure Time Distribution. The remaining step is to estimate the ideal arrival time probability distribution function $f_{i}^{A}$ for each commuter. I do this in three steps.

First, I fit a normal distribution on pre-experiment departure times, separately for each commuter. (I do this only once, before estimation.) Second, at each estimation step, I compute departure time choice probabilities $\pi_{i t}\left(h \mid h_{i t}^{A}, r, \theta\right)$ conditional on ideal departure time and route, as described above. This expression assumes no pricing, corresponding to the period before the experiment. This allows me to express the vector of departure time probabilities for route $r$ as a known linear transformation of the vector probabilities of all ideal arrival times, namely $\pi_{i t}(h \mid r)=\sum_{h^{A}} \pi_{i t}\left(h \mid h^{A}, r, \theta\right) f_{i}^{A}\left(h^{A}\right)$. I weight by observed route choice frequencies before the experiment and write the distribution of pre-experiment departure times in matrix form as $\pi_{i}=P_{i}(\theta, r) f_{i}^{A}$, where $\pi_{i}$ and $f_{i}^{A}$ are viewed as vectors over departure time and arrival time. The final step is inverting this relationship to obtain the vector $f_{i}^{A}$. I use non-negative least squares to solve
$\min _{f_{i}^{A}}\left\|\pi_{i}-P_{i}(\theta, r) f_{i}^{A}\right\|^{2}$ such that $f_{i}^{A} \geq 0$ and $\mathbf{1} \cdot f_{i}^{A}=1$ (Lawson and Hanson, 1974). This procedure does not introduce an incidental parameters problem because we are integrating over ideal arrival times drawn randomly from distribution (Kiefer and Wolfowitz, 1956).

GMM Estimation. I use two-step GMM with an optimal weighting matrix. Each stage is repeated with 120 random parameter starting conditions, to make convergence to a global minimum more likely. To account for the ideal arrival time inversion step in the estimation, I report $95 \%$ confidence intervals based on 120 bootstrap iterations, each estimated using 10 random starting conditions.

### 7.4 Travel Demand Estimation Results

Benchmark results are in Table 2.

Schedule Cost Estimates. Commuters have a small degree of flexibility to change their departure times. In the benchmark specification in column 1, early and late schedule costs are given by $\beta_{E}=552$ INR per hour ( 26.8 USD PPP) and $\beta_{L}=344$ INR per hour (16.7 USD PPP). These numbers are estimated using the full model with departure time and dynamic route choice, using experimental moments from the peak-hour pricing and route charges treatments.

To explain what these numbers imply in terms of behavior, I use the estimated model to simulate the individual response to a linearly increasing departure time charge $p^{D}(h)=p h$. When $p$ is the average wage ( 165 INR per hour), commuters leave 3.9 minutes earlier on average, a detectable but modest response. When $p$ is double the wage, commuters leave 8.7 minutes earlier on average. This response rises steeply as $p$ approaches $\beta_{E}$.

In the estimated model, commuters take advantage of travel time savings depending on the slope of the travel time profile. Commuters arrive on average up to 2 minutes early (before the ideal arrival time) when they travel before the peak, and up to 5 minutes late when they travel after the peak.

There are few estimates of schedule costs in the transportation economics literature to compare with. The canonical reference is Small (1982), who finds $\beta_{E} / \alpha=0.61$ and $\beta_{L} / \alpha=2.4$. (See also Bento et al. (2020).) My estimates in Table 2 are 0.91 (bootstrapped $95 \%$ CI [0.37, 2.52]) and 0.56 ( $95 \%$ CI $[0.31,2.0]$ ) and I cannot reject equality ( $\beta_{E}>\beta_{L}$ in $62 \%$ of bootstrap runs). Note that this symmetry may reflect preference heterogeneity. In a richer model where commuters differ in schedule costs, my experiment may capture early costs $\beta_{E}$ for commuters who already travel early (who are more likely to travel during the early "ramp" of the congestion charge profile), and late costs $\beta_{L}$ for late travelers. Given my focus on policies that incentivize traveling away from the peak-hour, these parameters are still policy-relevant.

Estimated schedule costs are robust to a range of assumptions on the value of travel time. In columns 2 and 3 of Table 2I estimate a model of departure time with a single short route $(r=0)$, and I calibrate VOTT to either $50 \%$ or $100 \%$ of the average wage. Estimated schedule costs are very similar. Conversely, the estimated VOTT is very similar in the dynamic route choice model without
departure time described at the end of section 4.2 Overall, the interaction between the departure time and route choice model components is negligible numerically.

Schedule costs depend primarily on commuter departure time responses to peak-hour charges (Figure A33). In panel A, I compute the Jacobian, showing that the early schedule cost $\beta_{E}$ most strongly affects moments $m(h)$ for departure times around the early ramp, and late cost $\beta_{E}$ most strongly affects moments around the late ramp. In panel B, I use the scaled sensitivity measure from Andrews et al. (2017), which measures how an estimated parameter depends on changes in the value of one of the moments (Appendix A.5). The same picture emerges: the moments $m(h)$ that affect $\hat{\beta}_{E}$ the most are around $h=-1.5$ hours, while those that affect $\hat{\beta}_{L}$ the are around $h=+1.5$ hours. A higher logit scale parameter $\sigma^{D T}$ means noisier departure time choices, which leads to a more dispersed response to pricing around pricing kink points at $\pm 1.5$ hours (not shown).

The model propagates reduced form moment uncertainty to parameter estimates in a relative transparent manner. To see this, consider the departure time substitution patterns shown in panel A of Figure A1 and panel A of Figure A2 If this profile were uniformly attenuated by a factor of two, estimated schedule costs would be $\beta_{E}=788$ and $\beta_{L}=446$, which are respectively $43 \%$ and $30 \%$ higher than the benchmark estimates.

The model does a good job of matching the experimental changes in volume of trips, notably at the $\pm 1.5$ hour kink points (Figure A2 panel A). It also matches well the control distribution of departure times (panel B).

Value of Travel Time (VOTT) Estimates. The estimated value of travel time is 609 INR per hour (29.5 USD PPP) or $369 \%$ of the average hourly wage reported in the survey (Table 22). This relatively large value indicates that commuters in Bangalore view additional driving time as highly undesirable.

The transportation economics conventional consensus for rich countries is that VOTT lies between $50 \%$ and $100 \%$ of the wage (Wardman, 1998). While many estimates are based on stated preferences, a method that underestimates VOTT (Small et al. 2005), recent experimental and quasi-experimental estimates of the value of wait time in ride-share settings find estimates in a similar range (Goldszmidt et al. 2020; Buchholz et al. 2020). Experimental estimates of the value of travel time in urban contexts in developing countries are not readily available.

The value of travel time is estimated separately from the cost of switching routes, which is $\gamma=80$ INR, or around half the hourly wage. If I estimate a static route choice model with the switching cost set to zero, using route choice probabilities with and without charges, VOTT increases significantly to 2,200 INR per hour (column 1 in Table A9). This model is rejected by the data, because it predicts no route choice persistence. In the benchmark model, switching costs are symmetric. If, instead, I assume that switching away from the short route $(r=0)$ is twice as costly $\left(\gamma_{01}=2 \gamma_{10}=2 \gamma\right)$, VOTT is estimated at 1, 486 INR per hour.

Three key route choice moments help to jointly estimate VOTT $\alpha$, the route switching cost $\gamma$, and the logit parameter $\sigma^{R}$. These moments correspond to detour route choice probabilities before the experiment (control), while charges are in effect (treatment), and after charges end (persistence). Table A11shows the Jacobian of the three moments with respect to the three parameters. The key
point is that a higher VOTT lowers detour choice during and after the experiment roughly similarly, while a higher switching cost affects persistence much less. Increasing the logit parameter increases all three moments uniformly, because it increases the importance of idiosyncratic factors. The same pattern holds in the benchmark model, in the model without departure time, and in a simple version of the dynamic route choice model.

Note that $\alpha$ is denominated using travel time as measured by Google Maps, and study participant perceptions of travel time differences are larger. Hence, the value of subjective time will be lower. The average detour is 6.5 minutes according to Google Maps. In a phone survey conducted during the experiment, the median and average self-reported detour durations were 11.7 and 13.6 minutes.

Inattention to the road pricing experiment may affect these estimates. In a phone survey, around half of treatment group respondents do not remember features of their treatment (Table SM1). Reestimating the benchmark model assuming that each participant is independently inattentive to congestion charges with probability $50 \%$ leads to lower VOTT, 330 INR per hour (Table A9 column 4). It is difficult to know how much of inattention reflects aspects specific to this experiment that would not generalize to a real-world policy, and how much reflect high values of preference parameters.

The value of travel time estimated here can be most naturally applied to short-term commuter responses to similar congestion area policies that induce a detour option. It is also relevant for assessing the disutility induced by temporary road closures, for example due to construction. In the rest of this paper, I will use the estimated VOTT (as well as a wide range of robustness values) to value improvements in travel time due to a less crowded peak-hour.

The benchmark model matches well the dynamic path of detour route choice in the two route treatment groups (Figure A2 panel C). I also show that the model matches well the route choice heterogeneity by detour duration, which is not targeted in estimation (panel D ).

Model Identification Check, Finite Sample Estimation, and Robustness As a numerical analogue of model identification, I show that the estimation procedure recovers true parameters using simulated data. For this exercise, for each random vector of model parameters, I simulate model choice data for the same set of study participants, assuming that individual choice probabilities are perfectly observed. I then estimate the model using this synthetic data. Estimated parameters track true parameters almost perfectly (Figure A4 red circles).$^{7}$

To study the finite sample properties of the estimation procedure, I repeat the exercise simulating random choices, holding the number of observations per participant exactly the same as in the real data. For every parameter, estimated parameters are positively correlated with true parameters, with slope most often close to 1 (Figure A4 blue triangles, and Table A12p).

The results are robust to a wide range of assumptions on the discount factor (Table A10). The key parameters are very similar for $\delta \in[0.5,0.99]$. I also estimate $\delta$ using an additional moment that captures the average transition probability from route 0 to route $18^{8}$

[^7]In order to focus on experimental variation in the route choice moments, I include time fixed effects that enter the detour route utility $(r=1)$ in equation (4). The terms $\eta_{t}$ are switched on for weeks $t=1,2,3,4$ during the experiment, for all commuters. (For departure times, the model already includes very rich individual level heterogeneity through the ideal arrival time distribution.) All estimates are similar to the benchmarks results, but the VOTT estimate is significantly less precise.

Finally, I consider a more restrictive model where all commuters have the same, time-invariant ideal arrival time $h^{A}$. Schedule costs are higher and very imprecisely estimated. This model offers a poor fit for the distribution of departure times in the control group (not shown).

Overall, the travel demand model does a good job fitting how commuters responded to the congestion charge experiments. The results indicate that commuters are moderately inflexible changing their schedules by leaving earlier or later locally around their departure times. The value of travel time estimates in Bangalore are higher than the typical $50-100 \%$ of the average wage. In order to quantify the welfare impacts of congestion mitigating policies, it is also necessary to know how travel times respond to aggregate changes in driving patterns.

Income Heterogeneity Many previous studies in other countries find that travel preferences scale with income (Wardman, 1998). This is important because heterogeneity in travel preferences has both efficiency and distributional consequences. In my experiment, I cannot detect heterogeneous effects by self-reported wage in either treatment (column 3 in TableSM6and column 2 in TableSM7, although this exercise is likely under-powered given sample sizes. With a similar caveat, I do not find evidence of differences in attention to the experiment between low- and high-wage participants (Table SM1. I re-estimate the demand model imposing that travel preference parameters are proportional to self-reported wage, and I find similar but less precisely estimated mean parameters (Table A9, column 5). I return to income heterogeneity in policy simulation.

## 8 The Road Traffic Congestion Technology

Each additional vehicle on the road leads to slower road speeds. I now quantify this external cost in Banglaore using all the GPS trip data collected during the study and real-time Google Maps driving time data from the same period 9

The main empirical strategy is to use the significant within-day variation in city-wide traffic density to measure the causal impact of traffic density on speeds. I will argue that, to a first approximation, the large shifts in demand for travel at different times of the day trace out the supply curve for road speed, which I call road technology.
utility, for participants who are informed that they will be charged in the last week in the experiment Abbring and Daljord, 2020). In practice, the experiment did not include a pure control group, and the simulated anticipatory response is small for a wide range of values of $\delta$.
${ }^{9}$ Driving also imposes other external costs: pollution emissions, pollution exposure, accidents, etc. Here I focus on the impact on higher (and less reliable) driving times.

The relationship of interest between travel delay and traffic density is

$$
\begin{equation*}
X_{t h}=\lambda_{0}+\lambda_{1} \widetilde{D}_{t h}+\varepsilon_{t h} \tag{8}
\end{equation*}
$$

where $X_{t h}$ is instantaneous travel delay (inverse speed, measured in minutes per kilometer) on day $t$ at hour $h, \widetilde{D}_{t h}=\frac{D_{t h}}{\bar{N}(\bar{T} / 24)}$ is citywide traffic density $D_{t h}$ at time $h$ normalized by the average number of daily trips $\bar{N}$ and average trip duration $\bar{T} / 24$, and $\varepsilon_{t h}$ is an error term. (I use $\bar{T}=0.5$ hours.)

To measure the quantity of driving, I use 117,527 trips coded from GPS data from 1,747 app users, covering 185 calendar dates and 44,034 user-days with travel information. (This sample includes but is not restricted to the experimental sample.) I use this to construct $D_{t m}^{S}$, the number of (in-sample) trips that are ongoing at minute $m$ on day $t$, which I then average at the hour level to get $D_{t h}^{S}$. To account for the changing number of app users over time, I normalize $D_{t h}^{S}$ by the number of app users active that week. I assume that in-sample density is a representative, if possibly noisy, measure of citywide density. This implies that $\widetilde{D}_{t h}^{S}$ is a noisy measure of $\widetilde{D}_{t h}$, which may lead to attenuation bias in (8) 10

My main data source for travel delay is real-time Google Maps travel delay data collected every 20 minutes on a fixed set of 30 routes in the study area (in both directions) over the same calendar period. This is a good proxy for instantaneous speed because the routes are short at 2.8 km on average. As a different outcome measure, I compute trip-level travel delay directly from the GPS data.

To address simultaneity concerns in equation (8) as well as mismeasurement in the traffic flow measure $\widetilde{D}_{t h}$, I use predictable within-day variation as a shifter of normalized density. In most analyses, I compute travel delay $X_{h}$ and traffic inflow $\widetilde{D}_{h}^{S}$ at the hourly level $h$, averaging over days $t$, and estimate the relationship $X_{h}=\lambda_{0}+\lambda_{1} \widetilde{D}_{h}^{S}+\varepsilon_{h}$. This is closely related to 2SLS estimates of (8) using hour dummies as instruments for $\widetilde{D}_{t h}^{S}$, which I also report.

Travel delay is well explained by a linear function of traffic density (Figure 4). The linear functional form is visible throughout the range of density, including at close to zero traffic and during the more congested daytime hours. An increase in density of $10 \%$ of the mean is associated with an increase of 0.1 minutes per kilometer (Table 3). Results are almost identical when weighting by inverse probability that a respondent is in the smartphone app sample (not shown). When estimating a power function $X_{h}=\lambda_{0}+\lambda_{1}\left(\widetilde{D}_{h}^{S}\right)^{\nu}+\varepsilon_{h}$, an exponent $\nu=1.06$ is outside the $95 \%$ confidence interval (column 2). The 2SLS specification gives similar results (column 3). The slope estimated based on variation across calendar dates is shallower (column 4), although comparing Sundays to all other weekdays suggests a similar slope (Figure SM5).

The entire distribution of travel delay computed from GPS trips, including the 90th percentile, scales linearly or sub-linearly as a function of traffic density (Figure A5. Panel A). This shows that the probability of severe traffic jams is not disproportionately higher during peak-hours.

Equipped with the estimated road technology, I can calculate the partial equilibrium impact

[^8]of an additional trip on total driving times in Bangalore. I solve the road technology model from equation (6) using the estimated equation (8) and my data on trips, and compute the total driving time summing up over all commuters. I solve the model again after adding an additional trip ${ }^{11}$

An additional 7 km long trip increases the total driving time in Bangalore by 1.3 minutes if the trip starts at 7 am , and by 14.6 minutes if it starts at 9 am . This is not the same as the trip's marginal social cost, which includes schedule costs and is calculated allowing other drivers to adjust Arnott et al. 1993. A 7 km long trip starting at 9 am takes 26 minutes, hence this congestion externality estimate is non-trivial. However, it is small relative to many previous estimates, including the bottleneck model, where the partial-equilibrium impact on travel times can be several times larger than the private cost Vickrey, 1969, Arnott et al. 1993).

Interpreting these results as the causal impact of driving on travel delay raises several potential concerns. First, the sample of trips may over-represent peak-hour traffic volumes (and hence underestimate the slope), for example due to recruitment times in gas stations. Note that recruitment time barely predicts trip departure time from GPS data. ${ }^{12}$ In any case, recruitment bias may go the other way, as surveyors worked continuously between $8 \mathrm{am}-1 \mathrm{pm}$ and $3 \mathrm{pm}-8 \mathrm{pm}$, yet the commuter arrival rate in gas stations is significantly higher during peak-hours. A related issue is if truck or other traffic is over-represented off-peak, meaning current results underestimate off-peak traffic volumes. I do not have the data to rule out this possibility. Note that Bangalore does not have explicit daytime truck traffic restrictions.

Another concern is that the true relationship is convex, but averaging over time or over space linearizes it. For example, the exact moment of the peak-hour may vary slightly on different days, leading to attenuation bias in traffic density. Figure A6 shows virtually identical results day by day, including on Sundays, when traffic volume is lower. These results bolster the case that the results trace out a technological relationship. In Figure A7, I count the number of ongoing trips by road artery and direction (arteries are shown in Figure SM1). Even for individual arteries, instantaneous travel delay appears linear in this measure of density, with a slope that is sometimes different than the citywide slope.

A general concern is that this analysis misses an omitted variable correlated with high peakhour demand and with faster peak-hour travel in equations (8). However, compelling examples are not obvious for Bangalore. For example, the study period was overwhelmingly dry and mild, so weather events correlated with peak-hours are unlikely. An example would be if traffic police disproportionately alleviates traffic during peak-hours. (However, this may also be considered a component of the road technology.) Some omitted variables might instead bias the relationship upward. For example, higher pedestrian flows during peak-hours may further slow traffic, biasing the slope up.

Peak-hour trips may be longer and hence faster, as shown in Couture et al. (2018), or peak-hour drivers may drive faster in general. I run trip-level quantile (median) regressions of trip delay on the

[^9]traffic density measure used above (Table SM9). These results are similar and shallower, including when controlling for trip length and commuter fixed effects.

Measuring a citywide relationship may underestimate externalities if commuters switch to lower externality routes during the peak hour, as in the Pigou-Knight two-route model (Walters 1961) ${ }^{13}$ To quantify this type of bias in Bangalore, I proceed in two steps. First, I show that the travel time change between 6 am and 9 am is a good proxy for a route's externality $\lambda_{1}$ from equation (8). In the artery-level data these two measures have $R^{2}=0.76$. This is useful because I can measure travel time profiles more widely. Second, for each frequent commuter in the experimental sample, I obtain all routes that are optimal for at least one departure hour. I then collect Google Maps travel time data along each route for all hours of the day ${ }^{14} 44 \%$ of commuters have a unique route, meaning all other routes are slower for all departure times. Even when more routes exist, the time profile slopes are similar (Figure A5 panel E). Denote $r_{i}(h)$ the optimal route for commuter $i$ at time $h, r_{i}^{*}$ the route with the steepest 6:30-9:30 slope, and slope $(r)$ the slope of route $r$. Usage of the steepest route $r_{i}(h)=r_{i}^{*}$ falls by $30 \%$ during peak-hours, showing that commuters indeed substitute away from high-externality routes. However, this effect is small, as slope $\left(r_{i}(h)\right)$ falls by $16 \%$ at most. To account for this bias, I later analyze policy counterfactuals in an equilibrium model with two routes, where one route has the citywide road technology I estimate here, and the other has a $15 \%$ or $30 \%$ steeper slope.

The results in Bangalore are broadly similar to those reported by Akbar and Duranton (2017) in Bogotá, Colombia (Figure A5 panel D). Akbar and Duranton (2017) construct traffic density using entire trips using a representative transportation household survey. These results suggest a more general conclusion about a shallow road traffic externality in urban road networks in developing countries ${ }^{15}$ Russo et al. (2019) and Yang et al. (2019) use loop detector data to characterize road traffic externalities in Rome and Beijing.

It is likely that at some higher level of traffic, citywide travel delay in Bangalore would become highly convex in additional traffic density, as streets overflow and vehicles block intersections. The results in this section suggest that these levels are not typically reached in the current equilibrium, even during peak-hours.

## 9 Policy Simulations

Equipped with preference estimates from the experiment and the calibrated road traffic congestion externality in Bangalore, in this section I simulate and compare the Nash equilibrium and social optimum in the model of peak-hour equilibrium from section 4.3. Appendix A.7 contains technical details.

Agents choose departure times based on equation (3), taking the travel time profile as given.

[^10]They have preference parameters $\alpha, \beta_{E}, \beta_{L}, \sigma^{D T}$ estimated in section 7 Each agent is a copy of a real study participant, with the same short route length and a fixed ideal arrival time drawn from the estimated distribution for that participant. In the benchmark model, departure time is the only margin of choice. I later introduce model extensions with route choice and with an extensive margin decision.

Travel times are determined endogenously as a function of the pattern of departures, using the linear relationship between density and instantaneous travel delay estimated in Table 3, column 1, based on equation (8). Recall that this specification induces a non-linear effect: higher density at one moment lowers instantaneous speed, which increases density later on. Travel time uncertainty is log-normally distributed with a standard deviation that is quadratic in the mean (Figure SM7).

The simulation focuses on morning peak-hour commuting trips. I assume these represent $20 \%$ of all trips in a given day in Bangalore. This factor is calibrated so that the unpriced Nash equilibrium peak travel delay is approximately $4 \mathrm{~min} / \mathrm{km}$, similar to Figure 1 . It also matches half the share of trips that are between home and work (Table A1. As I explain below, this parameter is an important factor for the deadweight loss of congestion (Figure A8 panel D).

In a Nash equilibrium, the distribution of agent departure probabilities and the profile of instantaneous travel delay are consistent. Welfare is defined as average expected utility. Externalities are defined around a certain equilibrium and allowing the other commuters to adjust (Arnott et al. 1993), and depend on departure time and trip length. The externality for agent $i$ of making a trip at departure time $h$ is the difference between equilibrium welfare assuming $i$ makes a trip starting at $h$, and equilibrium welfare when $i$ does not travel (both welfare terms exclude $i$ ). Because a trip affects traffic density for its entire duration, longer trips tend to have larger externalities. The social optimum is an equilibrium with Pigouvian charges $p(h, K)$ equal to the externality of a trip of length $K$ leaving at $h$. I assume no implementation costs and lump-sum redistribution of the entire revenue. This setup favors finding welfare benefits from optimal pricing.

I use an iterative procedure to compute a Nash equilibrium. At each step, a small fraction of commuters choose optimal departure times, and travel times adjust to the new pattern of departures. Convergence to equilibrium takes around 10 revisions per capita, and in practice the procedure identifies the same equilibrium for any starting conditions. This dynamic has a natural interpretation in terms of commuters revising their actions periodically.

To find the social optimum, I use a nesting iterative procedure to compute a series of Nash equilibria and update congestion charges. At each step, I update charges toward the externality at the current equilibrium. For computational reasons, I compute partial-equilibrium externalities (other commuters do not adjust). At the social optimum, I check that these coincide with fullequilibrium externalities, as implied by the envelope theorem. Even around the Nash equilibrium, the partial- and full-equilibrium externalities are highly correlated ( $R^{2}=0.96$ ).

Main Results. Figure 5 shows the profiles of average travel delay for the Nash equilibrium and for the social optimum. To construct it, for each departure time, I take the average over all commuters of the travel delay they would experience if they left at that time.

Optimal congestion charges lead to small but notable travel time reductions (Table 4 panel A).

Peak travel delay falls by around 0.4 minutes per kilometer and average travel time falls by 2.5 minutes per commuter. More commuters are induced to leave before and after the peak (Figure A8 panel B). For each simulation agent and their ideal arrival time draw, I compute the change in average departure time under the social optimum relative to the Nash equilibrium. The 10th and 90th percentiles are leaving 2.2 minutes earlier, and 9.6 minutes later. Intuitively, more commuters are induced to leave later because a trip has to either end before the peak hour or begin after in order to not contribute to peak hour congestion. These numbers are in the range of experimental responses to the departure time policy. Hence, these counterfactual results do not rely significantly on functional form extrapolations.

The Pigouvian charges that implement the social optimum follow the shape of the peak-hour, and are approximately proportional to trip length (Figure A8 panel A). The maximum per-Km rate is around $25 \mathrm{INR} / \mathrm{Km}$.

The social optimum has smaller commuter welfare gains, because larger schedule costs offset around two thirds of the travel time gains. Welfare is 9.4 INR higher per commuter under the optimum (0.46 USD PPP), compared to total trip cost of 397 INR in the Nash equilibrium. The welfare gain from optimal pricing-i.e., the deadweight loss of congestion-amounts to $2.3 \%$ of the welfare in the Nash equilibrium. The $95 \%$ confidence interval of $(0.7 \%, 4.5 \%)$ is calculated by bootstrapping estimated preferences and independently drawing from the variance covariance matrix of the estimated road technology relationship.

Welfare gains are larger relative to the portion of trip cost above free-flow conditions. As a benchmark, in a model with homogeneous commuters and bottleneck road technology (Arnott et al. 1993), optimal pricing reduces trip costs above free-flow conditions by $50 \%$. In my estimated model, the welfare gain relative to free-flow is only $5.9 \%$, more than eight times smaller.

How are these gains distributed? Commuters who typically travel during the peak-hour gain the most in terms of travel time and schedule cost changes. For each commuter, let their "typical" departure time be the expected departure time in the Nash equilibrium. The change in expected travel time utility $-\alpha \mathrm{E} T(h)$ in the social optimum relative to the Nash equilibrium is generally positive and follows the shape of the peak-hour (Figure A9 panel A). The change in expected schedule utility $\mathrm{E}\left(-\beta_{E}\left|h+T-h_{i}^{A}\right|_{-}-\beta_{L}\left|h+T-h_{i}^{A}\right|_{+}\right)$is generally negative, and has local minima midway before the peak, and right after the peak.

However, peak-hour commuters also pay the highest congestion changes, over $25 \mathrm{INR} / \mathrm{Km}$ ( 0.34 $\mathrm{USD} / \mathrm{Km})$. On net, they are worse off under the social optimum, both with a flat rebate, and with a rebate proportional to trip length (Figure A9 panel B).

These results suggest that real-world, more forceful policies that attempt to cap peak-hour congestion may lower commuter welfare. Indeed, real-world policies are likely to include implementation costs, may not fully recycle the revenue, and are unlikely to charge the optimal time-varying fees.

The simulation model makes several strong assumptions. I do not take into account longer term preferences and adjustments, which may be different from the short-term responses measured in the experiment. As in the road technology estimation, I do not distinguish between the externalities generated by motorcycles and cars. Finally, this analysis ignores other traffic, including trips that are not between home and work, and bus passengers who would also benefit from reductions in
travel times ${ }^{16}$ The simulations also ignore bus and truck traffic, which may respond differently to similar congestion charges and may affect traffic differently. These calculations also do not account for other important social costs of congestion, such as pollution.

When commuter travel preferences are heterogeneous and proportional to the self-reported wage (as estimated in Table A9, column 5), the deadweight loss of congestion increases to $4.5 \%$ (Table 4 panel B). The distributional consequences depend on the rebate scheme, because low-wage commuters make trips that are $25 \%$ shorter on average. The low-wage group has similar net change in expected utility with a rebate proportional to trip length, and on average they gain more than the high-wage group with a flat rebate.

Which model components drive the low welfare gains from optimal pricing? I first consider preferences. Deadweight loss is increasing in VOTT (panel C), yet these differences are small, and it is below $1 \%$ if we assume that VOTT equals the average wage. Deadweight loss (as a fraction of welfare in the Nash equilibrium) is decreasing in schedule costs, whereas it is always one half in Arnott et al. (1993). ${ }^{17}$

Welfare gains from optimal pricing are very sensitive to the road technology, especially its slope at the peak. Recall that I assume that simulation trips account for $20 \%$ of all trips in a typical day in Bangalore, in order to match the peak travel delay of $4 \mathrm{~min} / \mathrm{Km}$. The elasticity of deadweight loss with respect to equilibrium peak excess travel delay is 2.3 (Figure A8 panel D). This means that if the total volume of trips were larger such that the Nash equilibrium peak travel delay were $4.5 \mathrm{~min} / \mathrm{km}$ instead of $4 \mathrm{~min} / \mathrm{km}$, deadweight loss would be $4.2 \%$ instead of $2.4 \%$. If peak travel delay were $3.5 \mathrm{~min} / \mathrm{km}$, deadweight loss would be $1.2 \%$.

In panel D, I replace the linear technology with a power with exponent of 0.5 or 1.5 . I use the estimated $\lambda_{0}$ and $\lambda_{1}$ from the benchmark linear equation 8 and only vary the exponent $\nu$. This leads to slopes of 0.35 and 2.2 at relative density of 2.13 , the highest level in the data (Figure A8 panel C). Deadweight losses become $0.1 \%$ and $11.6 \%$. This and the previous finding highlight the key role played by the density-based road technology in determining deadweight losses.

Model Extension. So far, traffic conditions were assumed homogeneous within the city. I next consider an equilibrium model with two routes of equal length and with different road technologies. Route $r=0$ has the benchmark technology. Based on Figure A5 panel E, I assume that route $r=1$ has a $15 \%$ or $30 \%$ steeper slope and hence higher externality. Commuters now choose route and departure time, as in section 4.2 Given my focus on steady state equilibrium, and computational considerations, I use the static route choice model with zero route switching cost. Note that externalities (and hence optimal charges) depend on route, departure time and trip length. This setup

[^11]is related to the Pigou-Knight model (Walters 1961). Figure A10 shows results. Throughout the peak-hour of the Nash equilibrium, the high-externality route 1 has slightly higher delay and is used slightly less 18 Under the social optimum, route 1 delay falls below the delay of route 0 . Overall, the welfare gain from optimal pricing is $35 \%$ or $70 \%$ higher than in the benchmark case.

So far, trip decisions are inelastic. Given the previous finding that the total volume of traffic affects deadweight loss, I next consider a model with an extensive margin decision (and a single route). Commuters choose whether to make a trip, and their departure time, based on a nested logit model with scale parameter $\eta$. The cost of not making the trip is given by a parameter $\omega>0$ (Appendix A.7).

In Table 5 I simulate this model for six chosen combinations of $(\omega, \eta){ }^{19}$ To assess which parameters are reasonable, each time I compute the percent reduction in traffic (number of trips) due to a flat 100 INR (4.8 USD PPP) fee imposed at the Nash equilibrium, and the implied elasticity with respect to total travel costs. (As a point of reference, in these simulations, average congestion charges at the social optimum vary between 95 INR and 190 INR.)

Commuter welfare gains are increasing in the extensive margin elasticity. For small elasticities of around 0.10 , welfare gains are around $2.3 \%$. Achieving welfare gains over $4 \%$ requires elasticities above 1, or a $27 \%$ reduction in traffic volume from the flat 100 INR fee.

These results suggest that the linear road technology also limits potential gains from reducing the total volume of road traffic, for plausible values of the extensive margin elasticity.

## 10 Discussion

This paper shows that in cities with road networks similar to Bangalore, optimal time-varying peakhour congestion pricing and similar quantity-based restrictions are unlikely to significantly improve commuter welfare as defined here.

Peak-hour pricing may be highly beneficial in other settings, such as where the externality is highly non-linear, and where differentiated pricing is feasible, e.g. tolling only certain lanes Hall, 2018, 2020). In addition, peak-hour pricing may help correct other externalities, for example relieving prolonged exposure to air pollution from vehicle exhaust. A detailed measurement of those localized externalities, and data on awareness of and willingness to pay to avoid these harms is necessary to study these issues.

This paper also suggests that road infrastructure investment-including adding road capacity as well as investments to make road network flows more efficient-may currently be at an inefficiently

[^12]low level. A particularly interesting possibility is that a more efficient urban road network and congestion pricing are complementary policies. This would be the case if, for example, using synchronized traffic lights would lead to a more convex relationship between traffic volume and speed, thereby making congestion pricing more valuable.

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## Figures

Figure 1: Average Travel Delay in the Study Region in Bangalore


Notes: This graphs plots average travel delay as a function of departure time, on 30 major routes (in both directions) across the study area of South Bangalore, by day of the week. Travel delay is the number of minutes to cover one kilometer, i.e. the inverse of speed. (A travel delay of 2 minutes per kilometer corresponds to 18.6 miles per hour.) The travel time and route length data is obtained from the Google Maps API. For each route, I queried the "real-time" travel time (with traffic) as predicted by Google, every 20 minutes between February 21st and September 14th, 2017. The sample excludes major holidays.

Figure 2: Impact of Departure Time Charges on the Distribution of Departure Times


Panel (B) Evening Peak
Notes: These graphs plot the impact of departure time charges on the number of trips and distribution of departure times. The sample is all non-holiday weekdays with good quality GPS data, excluding days outside Bangalore. In the post period, the sample is restricted to the departure time treatment period, either the first or the last three weeks. To construct each figure, I consider four groups, each combination of before or during the experiment and the control or treatment group, pooling together the information and control sub-treatments, and the high- and low-rate groups. Within each group, I compute the kernel density of trip departure times (relative to the midpoint of the congestion charge for each commuter) and multiply it by the average number of trips per day in that group. I then plot the difference-in-differences of these four curves, as well as point-wise $95 \%$ confidence intervals based on 1,000 commuter-level bootstraps. The Y axis measures the change in the number of trips per day in a one hour departure time window. This exercise does not take into account randomization strata. Figure A1 repeats the exercise restricting to commuting trips of regular commuters.

Figure 3: Impact of Route Charges on Average Detour Route Usage


Notes: This graph shows average detour route usage among commuting trips for frequent commuters in the route treatment sample ( $\mathrm{N}=222$ ). The sample is all trips between a commuter's home and work locations in either direction, and the key outcome is a dummy for whether the trip does not intersect the congestion area for that commuter. I average this outcome within for each commuter and time period. I then run a regression with time period and commuter fixed effects. The graph shows the coefficients for each week during the experiment, relative to before the experiment, separately for the "early" (charges in week 1) and "late" (charges in week 4) groups. The $95 \%$ confidence intervals are based on standard errors clustered at the commuter level.

Figure 4: Road Technology: Travel Delay Linear in Traffic Density


Notes: This graph shows that instantaneous travel delay is approximately linear in traffic density at the level of departure times. The traffic density measure uses GPS data for 117,527 trips from 1,747 app users on 185 weekdays. To compute traffic density, I count the total number of ongoing trips at any given minute of the day (on any day in the sample), on weekdays. I normalize by the number of trips and by $0.5 \cdot 24$ because the average trip duration is close to 30 minutes. Travel delay is derived from Google Maps data collected over 30 routes in South Bangalore (in both directions), every 20 minutes daily for 185 weekdays. I compute the average delay over all weekdays and routes for each departure time. I plot the linear fit together with confidence intervals based on Newey-West inference with 3 hours lag, for the entire sample (gray, solid line) as well as for daytime hours only (blue, dashed line). Table 3 reports corresponding regressions. Figure SM5 repeats this exercise at the level of calendar dates instead of departure times. Figures A6 and A7 repeat this exercise separately for specific calendar dates, and for specific road arteries.

Figure 5: Policy Simulation: Unpriced Nash Equilibrium and Social Optimum


Notes: This graph shows the profile of average travel delay under the simulated Nash equilibrium (black, dashed line) and under the social optimum (red, solid line). The social optimum is a Nash equilibrium implemented with Pigouvian (equilibrium-consistent) charges given by marginal social cost, which depends on trip length and departure time (Figure A8, panel A). To construct this figure, for each trip length $K$, I compute the trip travel time for each departure time, and divide it by $K$ to obtain travel delay. I then integrate over the trip length $K$ distribution.

## Tables

Table 1: Impact of Departure Time Charges on Daily Outcomes

|  | $(1)$ |  | $(2)$ | $(3)$ | $(4)$ |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Outcome | Total Hypothetical Rates Today | Number of Trips | Today |  |  |  |
| Time of Day | AM \& PM | AM | PM | AM \& PM | AM | PM |
| Commuter FE | X | X | X | X | X | X |
|  |  |  |  |  |  |  |
| Panel A. All Departure Time Sub-Treatments |  |  |  |  |  |  |
| High Rate $\times$ Post | $-12.29^{* *}$ | $-6.92^{*}$ | -5.36 | -0.07 | -0.02 | -0.04 |
|  | $(6.04)$ | $(3.77)$ | $(3.41)$ | $(0.14)$ | $(0.07)$ | $(0.07)$ |
| Low Rate $\times$ Post | -8.30 | -3.30 | -5.00 | -0.08 | -0.01 | -0.08 |
|  | $(6.14)$ | $(3.58)$ | $(3.80)$ | $(0.14)$ | $(0.07)$ | $(0.07)$ |
| Information $\times$ Post | 0.45 | 0.29 | 0.16 | 0.10 | 0.06 | 0.04 |
|  | $(5.41)$ | $(3.27)$ | $(3.33)$ | $(0.13)$ | $(0.06)$ | $(0.07)$ |
| Post | 0.39 | -1.36 | 1.76 | 0.02 | -0.02 | 0.05 |
|  | $(4.87)$ | $(2.85)$ | $(3.06)$ | $(0.11)$ | $(0.05)$ | $(0.06)$ |
| Observations | 15,585 | 15,585 | 15,585 | 15,585 | 15,585 | 15,585 |
| Control Mean | 96.33 | 48.08 | 48.25 | 3.04 | 1.15 | 1.29 |

Panel B. Any Departure Time Charge vs. Control or Information

| Charges $\times$ Post | $-10.55^{* *}$ | $-5.28^{* *}$ | $-5.27^{* *}$ | -0.12 | -0.04 | $-0.08^{*}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $(4.18)$ | $(2.51)$ | $(2.57)$ | $(0.10)$ | $(0.04)$ | $(0.04)$ |
| Post | 0.65 | -1.19 | 1.84 | 0.07 | -0.01 | 0.04 |
|  | $(3.94)$ | $(2.38)$ | $(2.54)$ | $(0.09)$ | $(0.04)$ | $(0.04)$ |
| Observations | 15,585 | 15,585 | 15,585 | 15,585 | 15,585 | 15,585 |
| Control Mean | 95.74 | 46.89 | 48.85 | 2.95 | 1.04 | 1.12 |

Notes: This table reports difference-in-differences impacts of the departure time sub-treatments on daily total hypothetical rates and the total number of trips. In the first three columns, the outcome is the sum over trips that day of the trip hypothetical rate. The hypothetical rate for a given trip is between 0 and 100 and is computed based on the trip departure time, the respondent's rate profile, and a peak rate of 100 for all respondents. (See Figure SM2 for an example of rate profile.) In the last three columns, the outcome is the number of trips that day. The sample is all non-holiday weekdays with good quality GPS data, excluding days outside Bangalore. Only good quality trips are included (see section SM.3). In the post period, the sample is restricted to the departure time treatment period, either the first or the last three weeks. Columns (2), (4) and (3), (6) restrict to trips in the morning interval ( $7 \mathrm{am}-1 \mathrm{pm}$ ) and the evening interval $(4-10 \mathrm{pm})$, respectively. "Charges" is a dummy for either low rate or high rate. All specifications include respondent and study cycle fixed effects, and Post is an indicator for the experiment period. The mean of the outcome variable in the control group during the experiment is reported for each specification. Standard errors in parentheses are clustered at the respondent level. ${ }^{*} p \leq 0.10,{ }^{* *} p \leq 0.05,{ }^{* * *} p \leq 0.01$

Table 2: Travel Demand Parameter Estimates

|  | (1) | (2) | (3) | (4) |
| :---: | :---: | :---: | :---: | :---: |
| Model: | Benchmark | Only Departure Time Calibrated VOTT |  | Only <br> Route Choice |
| $\beta_{E}$ : Schedule cost early (INR/hour) | $\begin{gathered} 552 \\ {[301,1539]} \end{gathered}$ | $\begin{gathered} 488 \\ {[214,956]} \end{gathered}$ | $\begin{gathered} 530 \\ {[250,1628]} \end{gathered}$ |  |
| $\beta_{L}$ : Schedule cost late (INR/hour) | $\begin{gathered} 344 \\ {[245,1262]} \end{gathered}$ | $\begin{gathered} 331 \\ {[223,2229]} \end{gathered}$ | $\begin{gathered} 329 \\ {[191,932]} \end{gathered}$ |  |
| $\alpha$ : Value of travel time (INR/hour) | $\begin{gathered} 609 \\ {[365,1210]} \end{gathered}$ | 82 | 165 | $\begin{gathered} 562 \\ {[357,1213]} \end{gathered}$ |
| $\gamma$ : Route switching cost (INR) | $\begin{gathered} 80.3 \\ {[43.2,112.2]} \end{gathered}$ |  |  | $\begin{gathered} 86.4 \\ {[42.2,106.0]} \end{gathered}$ |
| $\sigma^{D T}$ : Logit departure time | $\begin{gathered} 19.5 \\ {[1.3,68.0]} \end{gathered}$ | $\begin{gathered} 17.0 \\ {[1.0,73.9]} \end{gathered}$ | $\begin{gathered} 15.5 \\ {[1.2,89.9]} \end{gathered}$ |  |
| $\sigma^{R}$ : Logit route (upper nest) | $\begin{gathered} 57.9 \\ {[41.8,76.4]} \end{gathered}$ |  |  | $\begin{gathered} 57.6 \\ {[44.4,73.5]} \end{gathered}$ |
| Model Components: |  |  |  |  |
| Route choice model | Dynamic | - | - | Dynamic |
| Calibrated VOTT $\alpha$ | - | 50\% wage | 100\% wage | - |
| Departure time model | Yes | Yes | Yes | - |
| Moments: |  |  |  |  |
| Departure time (49) | Yes | Yes | Yes | - |
| Dynamic route choice (10) | Yes | - | - | Yes |

Notes: This table reports two-step GMM estimates of discrete choice travel demand models. The estimating equation, moments, data and procedure are described in section 7 Column 1 corresponds to the full model with departure time and dynamic route choice. Columns 2 and 3 use a departure time model with a single route (the short route, $r=0$ ) and calibrate VOTT to $50 \%$ and $100 \%$ of the average wage in the sample. The parameters $\left(\beta_{E}, \beta_{L}, \sigma^{D T}\right)$ are estimated using the set of 49 departure time moments. Column 4 corresponds to a model of dynamic route choice without departure time choice, estimated using the set of 10 dynamic route choice moments. For each model, I use 120 random initial conditions to find the minimum of the objective function. $95 \%$ confidence intervals from 120 bootstrap iterations are reported in parentheses.

Table 3: Road Technology: Travel Delay Linear in Traffic Density

|  | (1) | (2) | (3) | (4) |
| :---: | :---: | :---: | :---: | :---: |
| Dependent Variable: | Travel Delay Google Maps (min/km) |  |  |  |
| Sample: | Dep | me (h) | Date $\times$ Dep Time ( $t h$ ) | Date ( $t$ ) |
| Specification: | OLS | NLS | 2SLS | OLS |
| Traffic Density | $\begin{gathered} 1.01^{* * *} \\ (0.04) \end{gathered}$ | $\begin{gathered} 1.16^{* * *} \\ (0.10) \end{gathered}$ | $\begin{gathered} 0.95^{* * *} \\ (0.04) \end{gathered}$ | $\begin{gathered} 0.47^{* * *} \\ (0.04) \end{gathered}$ |
| Traffic Density Exponent $\nu$ |  | $\begin{gathered} 0.82^{* * *} \\ (0.11) \end{gathered}$ |  |  |
| Constant | $\begin{gathered} 2.09^{* * *} \\ (0.04) \end{gathered}$ | $\begin{gathered} 2.00^{* * *} \\ (0.05) \end{gathered}$ |  | $\begin{gathered} 2.60^{* * *} \\ (0.04) \end{gathered}$ |
| Observations | 24 | 24 | 3,474 | 185 |
| Traffic Density Std.Dev. | 0.76 | 0.76 | 0.86 | 0.24 |
| Adj. $R^{2}$ | 0.97 | 0.98 | 0.87 | 0.54 |

Notes: This table shows the relationship between travel delay and traffic density in Bangalore. See Figure 4 notes. In column 3, I compute traffic density separately for each date, further normalizing by the number of app users active in the same week. In column 4, I compute total traffic density on each date. Columns 1 and 4 report OLS regressions with Newey-West standard errors, with a three-hour lag in column 1 and a 14-day lag in column 4. Column 2 reports results from nonlinear regressions $X_{h}=\lambda_{0}+\lambda_{1}\left(\widetilde{D}_{h}^{S}\right)^{\nu}+\varepsilon_{h}$ with HAC standard errors with Newey-West kernel and three-hour lag. Column 3 reports 2SLS estimates where I instrument date-hour density with 24 hour dummies, with standard errors clustered two-way by date and hour. (In column 3, HAC standard errors with Newey-West kernel and three-hour lag are smaller.) Table SM10 repeats the analysis using travel delay computed from GPS data. ${ }^{*} p \leq 0.10,{ }^{* *} p \leq 0.05,{ }^{* * *} p \leq 0.01$

Table 4: Policy Simulations: Commuter Welfare Gains from Optimal Peak-Hour Pricing
$\left.\begin{array}{lcccc}\hline & (1) & (2) & (3) & (4) \\ \text { Improvement }\end{array}\right)$

Notes: This table compares the unpriced Nash equilibrium and the social optimum under different assumptions. Columns 3 and 4 report the improvement from the unpriced Nash to the social optimum, in levels and as a percentage of the baseline (Nash) value. Panel A describes the benchmark model with preferences as estimated from the experiment and the calibrated road technology. Travel times are calculated taking individual route length into account, and welfare is average expected utility, assuming charges are transferred lump-sum back to commuters, and no implementation costs. In rows 2 and 4 travel time and welfare are computed relative to "free-flow" benchmark, where travel delay is $2.09 \mathrm{~min} / \mathrm{km}$ and does not increase with traffic density. Agent preferences in Panel B correspond to those estimated in column 5 in Table A9. In Panel C, I vary the VOTT or early schedule cost parameters. In Panel D, I vary the exponent on traffic density in the road technology relationship (Figure A8, panel C). In panel E, I simulate a model with two routes that have different road technologies. Route $r=0$ has the benchmark road technology, while $r=1$ has $15 \%$ or $30 \%$ steeper slope and $7.5 \%$ or $15 \%$ lower intercept. In panels A and B, $95 \%$ confidence intervals are bootstrapped based on bootstrapped parameter vector estimates, and random draws from the road technology variance covariance matrix (Table 3, column 1).

Table 5: Policy Simulations: Equilibrium with Extensive Margin Decision

| Trip value <br> $\omega$ | Logit trip <br> parameter <br> $\eta$ | \% Traffic Reduction <br> from flat 100 INR fee | Implied elasticity <br> at flat 100 INR fee | Nash <br> Welfare (INR) | Improvement <br> at Social Optimum <br> (\% of Nash) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 600 INR | 20 | -0.31 | 1.26 | -394.2 | $4.4 \%$ |
| 800 INR | 20 | -0.08 | 0.24 | -394.3 | $2.2 \%$ |
| 1000 INR | 20 | -0.01 | 0.02 | -394.4 | $2.2 \%$ |
| 600 INR | 100 | -0.25 | 1.0 | -359.7 | $4.3 \%$ |
| 800 INR | 100 | -0.12 | 0.4 | -387.7 | $3.4 \%$ |
| 1000 INR | 100 | -0.04 | 0.1 | -393.4 | $2.5 \%$ |

Notes: This table reports commuter welfare gains from optimal congestion pricing and extensive margin elasticities for the model with an extensive margin trip decision (Appendix A.7). The implied elasticity is computed with respect to total travel costs (equal to negative commuter expected welfare) at the Nash equilibrium. The average trip probability is $\geq 97 \%$ at the Nash equilibrium for all parameter combinations except for $\omega=600$ INR and $\eta=100$, when it is $89 \%$. In these simulations, average congestion charges at the social optimum vary between 95 INR and 190 INR.

## A Online Appendix

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## A. 1 Departure Time Model Identification

In this section, I formally prove how identification of schedule costs and schedule heterogeneity in a departure time model depends on observing commuter reactions to congestion pricing. For analytical tractability, I proceed in a simplified model that maintains the key features of the full model: schedule preferences and a peak-hour (inverse U shaped) travel time profile.

For intuition, consider a commuter that we observe to leave at very different times on different days (as I document in Table A1). There are two ways this could arise. In the first scenario, the commuter has a unique ideal arrival time and high schedule flexibility. In this case, small idiosyncratic shocks have a large effect on departure times. In the second scenario, each day, the commuter draws an ideal arrival time from a dispersed distribution, but does not have much flexibility around that time.

These two cases are observationally equivalent for departure times, but they have different implications for how substitutable two departure times are to each other, on any given day. The key intuition for how congestion pricing leads to identification is that we can measure cross-price elasticities: how the probability of choosing departure time $h$ depends on infinitesimal pricing of departure time $h^{\prime}$.

## A.1.1 Simplified Departure Time Model

I assume that commuters have preferences directly over (continuous) departure times $h \in \mathbb{R}$. Unlike the main model where commuters have ideal arrival times, this assumption eliminates expectations over travel time uncertainty and greatly simplify the algebra.

Travel time is a (possibly degenerate) quadratic function of departure time. This captures the key shape of how travel time varies across the peak hour ${ }^{20}$ In most of the results below, schedule costs are quadratic and the ideal departure time is normally distributed. These assumptions rule out asymmetric (early/late) schedule costs yet deliver analytical tractability.

Given the focus on identification, I drop individual $i$ and time $t$ subscripts and assume that infinite data for a single individual is available. The utility for departure time $h$ is

$$
\underbrace{-\alpha T(h)-v\left(h-h^{D}\right)}_{u\left(h \mid h^{D}\right)}+\epsilon^{D}(h) .
$$

Here $v(\cdot)$ is the schedule penalty as a function of the deviation between departure time and the ideal departure time $h^{D} . \epsilon^{D}(h)$ are idiosyncratic shocks with scale $\beta^{-1}$ that give rise to continuous logit choice probabilities. The ideal departure time $h^{D}$ is distributed according to a cumulative distribution function $F$.

I assume that the value of travel time $\alpha$ is known and normalize it to $\alpha=1$. Note, if travel time is not constant, this rules out a trivial source of non-identification due to scale.

The conditional probability density of choosing departure time $h$ is given by the continuous logit density, and the unconditional density is given by integrating over $F$,

$$
\pi\left(h \mid h^{D}\right)=\frac{\exp \left(\beta u\left(h \mid h^{D}\right)\right)}{\int_{h^{\prime}} \exp \left(\beta u\left(h^{\prime} \mid h^{D}\right)\right) d h^{\prime}}, \text { and } \pi(h)=\int \pi\left(h \mid h^{D}\right) d F\left(h^{D}\right)
$$

## A.1.2 Two Non-Identification Results with Observational Data

Before outlining the main results, I prove a general non-identification result in a simple setting where travel time is a constant (later, I will assume quadratic) and the ideal departure time distribution is unrestricted.

In this case, we can write the observed departure time as the sum of two independent random variables, corresponding to the ideal departure time, and the optimal departure time conditional on the ideal departure time. This exact decomposition helps clarify the source of non-identification.

Proposition 1. Assume that travel time $T$ is a constant (does not depend on departure time $h$ ). Normalize $\beta=1$. Consider any family $V$ of schedule delay functions $v \in V$, with at least two elements $v_{1}, v_{2} \in V$ that differ on a non-zero measure set. Then, the schedule delay cost function $v(\cdot)$ is not identified given data on $\pi(h)$.

Proof. If $T$ does not depend on $h$, then $u\left(h \mid h^{D}\right)$ is only a function of the difference $h-h^{D}$. Hence, the optimal departure time random variable $h^{*}$ can be written as the sum of two independent random variables, $h^{*}=h^{D}+\underbrace{h^{*}-h^{D}}_{h^{E}}$, where the pdf of $h^{E}$ is

$$
G\left(h^{E}\right)=\frac{\exp \left(-v\left(h^{E}\right)\right)}{\int_{h} \exp (-v(h)) d h}
$$

[^13](Note: if $v$ is quadratic then $h^{E}$ is normally distributed.)
Consider two different schedule delay functions $v_{1}(\cdot)$ and $v_{2}(\cdot)$ and let $h_{1}^{E}$ and $h_{2}^{E}$ denote two independent random variables that have the corresponding pdfs $G_{1}$ and $G_{2}$.

Setting the ideal departure time distributions $h_{1}^{D} \sim G_{2}$ and $h_{2}^{D} \sim G_{1}$ (note that indices are switched) implies that the observed optimal departure time random variables $h_{1}^{D}+h_{1}^{E}$ and $h_{2}^{D}+h_{2}^{E}$ have the same distribution. Hence, the schedule cost function $v(\cdot)$ is not identified.

The identification failure does not depend on constant travel time. I next prove the main nonidentification result, in a model that is more strongly parametrized and where travel time is humpshaped, which captures the peak-hour travel time profile. I make three functional form assumptions.

Assumption 1. $T(h)$ is quadratic, $T(h)=T_{\max }-a h^{2}$ with $a>0$. Without loss of generality and for convenience I will set $T_{\max }=0$.

Assumption 2. Schedule costs are quadratic, $v\left(h-h^{D}\right)=s\left(h-h^{D}\right)^{2}$ with $s>a$.
( $s>a$ means that schedule cost dominate, and it implies that the commuter chooses departure times with negative travel time-very early or very late departure time-with very low probability.)

Assumption 3. The ideal departure time is normally distributed, $h^{D} \sim N(\mu, \sigma)$.
Proposition 2. Fix the shape of the travel time profile a and maintain the VOTT normalization $\alpha=1$. Under assumptions $1-3$, the demand model parameters $(\beta, s, \mu, \sigma)$ are not identified with data on observed departure times.

This is not a trivial non-identification result due to scale, because VOTT $\alpha$ is normalized to 1 , and travel time is not constant.

The proof will show that it is possible to explain the same observed distribution of departure times by increasing schedule costs and increasing the position and the spread of the ideal departure time distribution.

Proof of Propostion 2. I show that $\pi(h)$ is a normal distribution. Its mean and variance depend on four variables $(\beta, s, \mu, \sigma)$. Hence, the model is under-identified with two degrees of freedom.

The utility functions is (recall that the value of time spent driving $\alpha$ is normalized to 1 )

$$
u\left(h \mid h^{D}\right)=a h^{2}-s\left(h-h^{D}\right)^{2}+\epsilon^{D}(h)
$$

Choice probabilities are given by

$$
\begin{aligned}
\pi(h) & =\int \pi\left(h \mid h^{D}\right) d F\left(h^{D}\right) \\
& =\int \frac{e^{-\beta\left(-a h^{2}+s\left(h-h^{D}\right)^{2}\right)}}{\int_{-\infty}^{\infty} e^{-\beta\left(-a\left(h^{\prime}\right)^{2}+s\left(h^{\prime}-h^{D}\right)^{2}\right)} d h^{\prime}} \cdot \frac{1}{\sqrt{2 \pi} \sigma} e^{-\frac{1}{2}\left(\frac{h^{D}-\mu}{\sigma}\right)^{2}} d h^{D} \\
& =\frac{1}{\sqrt{2 \pi} \sqrt{\frac{s^{2} \sigma^{2}}{(s-a)^{2}}+\frac{1}{2 \beta(s-a)}}} \exp \left(-\frac{1}{2} \frac{\left(h-\frac{s \mu}{s-a}\right)^{2}}{\frac{s^{2} \sigma^{2}}{(s-a)^{2}}+\frac{1}{2 \beta(s-a)}}\right)
\end{aligned}
$$

This is a normal distribution with mean $\frac{s \mu}{s-a}$ and variance $\frac{s^{2} \sigma^{2}}{(s-a)^{2}}+\frac{1}{2 \beta(s-a)}$.

## A.1.3 Identification with Congestion Pricing Variation

I now study identification when we also observe choice probability distributions $\pi(\cdot \mid p(\cdot))$ in response to any possible pricing function $p(h)$.

Observing responses to pricing helps identify the cross-price elasticities for different departure times. This helps resolve the ambiguity discussed in the previous section, because different combinations of departure time distributions and conditional choice probabilities have different implications for cross-price elasticities.

The key object of interest is the impact of an "impulse" price function on choice probabilities. Slightly abusing notation (skipping a formal limit argument), we study "Kronecker delta" impulse pricing functions at $h$ given by $p(x ; h, \lambda)=\lambda 1(x=h)$ and study the effect of increasing $\lambda$ around $\lambda=0$ for given $h \neq h^{\prime}$ :

$$
\left.\frac{d \pi\left(h^{\prime} \mid p(\cdot ; h, \lambda)\right)}{d \lambda}\right|_{\lambda=0}=\frac{d}{d \lambda} \int \frac{\exp \left(\beta u\left(h^{\prime} \mid h^{D}\right)\right)}{\int_{h^{\prime \prime}} \exp \left(\beta u\left(h^{\prime \prime} \mid h^{D}\right)-\beta p\left(h^{\prime \prime} ; h, \lambda\right)\right)} d F\left(h^{D}\right)
$$

For $h \neq h^{\prime}$ and evaluating at $\lambda=0$ this simplifies to

$$
\beta \int \pi\left(h^{\prime} \mid h^{D}\right) \pi\left(h \mid h^{D}\right) d F\left(h^{D}\right)
$$

where $\pi\left(\cdot \mid h^{D}\right)$ denotes the conditional probabilities in the absence of pricing $(\lambda=0)$.
This expression shows that, for fixed $h-h^{\prime}$, when conditional probabilities are concentrated (e.g. when $\beta$ is high and/or the schedule cost function is steep around the ideal departure time), the cross-elasticities are close to zero. Intuitively, this suggests that knowing cross-elasticities for all $h$ and $h^{\prime}$ solves the identification problem.

I now formally prove identification in the particular case considered in Result 2.
Proposition 3. Fix the shape of the travel time profile a. Under assumptions 1-3, the model parameters $(\beta, s, \mu, \sigma)$ are identified with data on observed departure times and cross-elasticities for $h \neq h^{\prime}$.

Proof. Substituting the utility function and normal distribution for $h^{D}$ in the expression for crosselasticity, and computing integrals using Mathematica, yields

$$
\begin{aligned}
\beta \int \pi\left(h^{\prime} \mid h^{D}\right) \pi\left(h \mid h^{D}\right) d F\left(h^{D}\right) & =\beta^{2}(s-a)^{\frac{1}{2}}\left(s-a+4 \beta s^{2} \sigma^{2}\right)^{-\frac{1}{2}} \\
& \exp \left(\frac{(s-a)\left(2 \beta s \sigma^{2}\left(h^{\prime}+h\right)+\mu\right)^{2}}{2 \sigma^{2}\left(s-a+4 \beta s^{2} \sigma^{2}\right)}-(s-a) \beta\left(\left(h^{\prime}\right)^{2}+h^{2}\right)-\frac{\mu^{2}}{2 \sigma^{2}}\right) .
\end{aligned}
$$

Taking log and grouping terms in a polynomial of $h$ and $h^{\prime}$ gives

$$
\begin{aligned}
\log \left(\beta \int \pi\left(h^{\prime} \mid h^{D}\right) \pi\left(h \mid h^{D}\right) d F\left(h^{D}\right)\right)= & -2 \beta(s-a)\left(\left(h^{\prime}\right)^{2}+h^{2}\right)+ \\
& \frac{4 \beta^{2} s^{2} \sigma^{2}(s-a)}{s-a+4 \beta s^{2} \sigma^{2}}\left(h^{\prime}+h\right)^{2}+ \\
& \frac{4 \beta \mu s(s-a)}{s-a+4 \beta s^{2} \sigma^{2}}\left(h^{\prime}+h\right)- \\
\operatorname{Ln}\left(s-a+4 \beta s^{2} \sigma^{2}\right)+ & 3 \operatorname{Ln}(s-a)+\frac{\mu^{2}(s-a)}{\sigma^{2}\left(s-a+4 \beta s^{2} \sigma^{2}\right)}-\frac{\mu^{2}}{\sigma^{2}}+4 \operatorname{Ln}(\beta) .
\end{aligned}
$$

We have four coefficients and four unknowns $(\beta, s, \mu$ and $\sigma)$. It is algebraically tedious but conceptually straightforward to check that this system of equations has a unique solution.

## A. 2 Route Choice Model Identification

To provide intuition for how VOTT and the route switching cost are separately identified using data from the route choice experiment, I analyze a version of the dynamic route choice model without departure time from section 4.2 I further assume no time discounting $(\delta=0)$.

Consider three time periods. At $t=0$ the model is in steady state. At $t=1$ the short route $(r=0)$ is unexpectedly charged $p$. At $t=2$ the route is no longer charged. Denote $\pi_{t}\left(r_{t-1} \rightarrow r\right)$ the probability to use route $r$ at time $t$ if the $t-1$ route was $r_{t-1}$ when there is no pricing, and $\pi_{t}\left(r_{t-1} \rightarrow r \mid p\right)$ with pricing $p$. Because there is no discounting, we have the following expressions for relative transition probabilities:

$$
\begin{array}{cl}
\frac{\pi_{0}(0 \rightarrow 0)}{1-\pi_{0}(0 \rightarrow 0)}=\frac{\exp (0)}{\exp \left(\frac{-\gamma-\alpha \Delta T}{\mu}\right)} & \frac{\pi_{0}(1 \rightarrow 0)}{1-\pi_{0}(1 \rightarrow 0)}=\frac{\exp \left(\frac{-\gamma}{\mu}\right)}{\exp \left(\frac{-\alpha \Delta T}{\mu}\right)} \\
\frac{\pi_{1}(0 \rightarrow 0 \mid p)}{1-\pi_{1}(0 \rightarrow 0 \mid p)}=\frac{\exp \left(\frac{-p}{\mu}\right)}{\exp \left(\frac{-\gamma-\alpha \Delta T}{\mu}\right)} & \frac{\pi_{1}(1 \rightarrow 0 \mid p)}{1-\pi_{1}(1 \rightarrow 0 \mid p)}=\frac{\exp \left(\frac{-p-\gamma}{\mu}\right)}{\exp \left(\frac{-\alpha \Delta T}{\mu}\right)}
\end{array}
$$

It is easy to solve for the parameters $\alpha, \gamma, \mu$ if these transition probabilities are known. Next, I show that these parameters are also unique determined by the detour route usage rates $S_{t}$ in periods $t=0,1,2$. These numbers satisfy the following equations (note that $t=0$ and $t=2$ have the same transition probabilities)

$$
\begin{aligned}
S_{0} \pi_{0}(0 \rightarrow 1) & =\left(1-S_{0}\right) \pi_{0}(1 \rightarrow 0) \\
S_{1} & =S_{0} \pi_{1}(0 \rightarrow 0 \mid p)+\left(1-S_{0}\right) \pi_{1}(1 \rightarrow 0 \mid p) \\
S_{2} & =S_{1} \pi_{0}(0 \rightarrow 0)+\left(1-S_{1}\right) \pi_{0}(1 \rightarrow 0)
\end{aligned}
$$

It is tedious but straightforward to show that these three equations uniquely determine $\alpha, \gamma, \mu$.

## A. 3 Route Charge Treatment Regression Analysis

For the regression analysis of the route experiment, I focus on the early treatment group and the period before the experiment and the first two weeks during the experiment. I use the following specification:

$$
\begin{equation*}
y_{i t}=\gamma^{A} \cdot T_{i}^{\text {Early }} W_{t}^{1}+\gamma^{A, P} \cdot T_{i}^{\text {Early }} W_{t}^{2}+\mu_{t}+\alpha_{i}+\varepsilon_{i t} \tag{9}
\end{equation*}
$$

The coefficients of interest are $\gamma^{A}$ and $\gamma^{A, P}$, which measure the impact of route congestion charges in the early charges group, and the persistence effect one week later, relative to similar commuters who anticipate that they will be treated in the fourth week of the experiment.

Panel A of Table A7 shows the impact of route charges on detour usage at the trip level. The sample is all trips between home and work. The results show a large increase of 27 percentage points during the first week in the experiment among the early treatment group, who faced charges that week. By comparison, only $11 \%$ of participants in the late group chose the detour that week. The second column shows that more than a third of this effect size persists one week later. Charges do not have a significant effect on the number of trips per day (columns 3 and 4). This means that there is no evidence that commuters reduce the number of trips to avoid route congestion charges, and the previous effects are driven by route switching.

I next analyze how baseline experience with detour routes affects the impact of charges. In Panel B, I restrict to commuters who use a detour route between home and work (or between work and home) at least once before the experiment. In general, the results from Panel A are amplified in this sample. Baseline usage is higher, as are the impact of charges ( 41 percentage points) and the persistence effect.

## A. 4 Travel Demand Estimation

## A.4.1 Choice Probabilities

In the benchmark model with dynamic route choice and departure time choice, the departure time choice probabilities conditional on the chosen route (with $p_{i t}(h, r)=0$ ) is given by

$$
\begin{equation*}
\pi_{i}\left(h \mid r, h_{i t}^{A}\right)=\frac{\exp \left(\left(\sigma^{D T}\right)^{-1} \operatorname{Ev}\left(h, \mathcal{T}_{i}(h, r), h_{i t}^{A}\right)\right)}{\sum_{h^{\prime}} \exp \left(\left(\sigma^{D T}\right)^{-1} \operatorname{Ev}\left(h^{\prime}, \mathcal{T}_{i}\left(h^{\prime}, r\right), h_{i t}^{A}\right)\right)} \tag{10}
\end{equation*}
$$

These expressions show that the full model collapses to the single-route departure time choice model given by (3) when we condition on route and ideal arrival time. Similar expressions apply when we include pricing $p_{i t}(h, r)$.

In the full model, the expected utility of choosing route $r$ is

$$
\mathrm{E} u_{i t}\left(r \mid h_{i t}^{A}, r_{i t-1}\right)=\sigma^{D T} \log \left(\sum_{h} \exp \left(\left(\sigma^{D T}\right)^{-1} \operatorname{Ev}\left(h, \mathcal{T}_{i}(h, r), h_{i t}^{A}\right)\right)\right)-\gamma \mathbf{1}\left(r \neq r_{i t-1}\right)+\delta V_{i t+1}(r)
$$

This includes the "logsum" or 'inclusive value" term over departure times. In the upper nest, this
leads to route choice probabilities (conditional on $h_{i t}^{A}$ )

$$
\pi_{i t}\left(r \mid h_{i t}^{A}, r_{i t-1}\right)=\frac{\exp \left(\left(\sigma^{R}\right)^{-1} \mathrm{E} u_{i t}\left(r \mid h_{i t}^{A}, r_{i t-1}\right)\right)}{\exp \left(\left(\sigma^{R}\right)^{-1} \mathrm{E} u_{i t}\left(0 \mid h_{i t}^{A}, r_{i t-1}\right)\right)+\exp \left(\left(\sigma^{R}\right)^{-1} \mathrm{E} u_{i t}\left(1 \mid h_{i t}^{A}, r_{i t-1}\right)\right)} .
$$

Unconditional probabilities follow by integrating over the ideal arrival time distribution $f_{i}^{A}$.

## A.4.2 GMM Moments That Exploit Experimental Variation

The two-step optimal GMM estimation finds the parameter vector $\theta=\left(\alpha, \beta_{E}, \beta_{L}, \gamma, \sigma^{D T}, \sigma^{R}, \eta_{\text {early }}\right)$ that solves $\min _{\theta} \hat{g}(\theta)^{\prime} \hat{W} \hat{g}(\theta)$ where the moment function $g(\theta)$ is described below, and $\hat{W}$ is the estimated optimal weighting matrix from the second step. (For the first step I use $\hat{W}=I$.)

Departure Time Moments. The first 49 moments match the difference in difference in departure time market shares, between the departure time treatment and control groups, during the experiment relative to before. Let $k$ index the 5-minute-step departure time grid between -120 and +120 minutes relative to the rate profile peak. Denote $P_{i k}^{D T}\left(\theta, p_{i t}\right)$ the probability that the $k$ th departure time is optimal when departure time and route pricing is $p_{i t}$. In the data, define $\widetilde{P}_{i k}^{D T}($ pre $)$ and $\widetilde{P}_{i k}^{D T}$ (post) the fractions of trips starting in a 5-minute bin around the $k$ th departure time for $i$ in pre- and post- periods, respectively. The $k$-th moment is:

$$
g_{i}^{k}\left(\theta, p_{i t}\right)=(-1)^{1-T_{i}^{D T}}\left[\left(\widetilde{P}_{i k}^{D T}(\text { post })-\widetilde{P}_{i k}^{D T}(\text { pre })\right)-\left(P_{i k}^{D T}\left(\theta, p_{i t}\right)-P_{i k}^{D T}(\theta, 0)\right)\right]
$$

where $T_{i}^{D T}$ is an indicator for departure time charges.
Route Moments. Ten moments match route choice market shares during five periods (before the experiment, and four weeks during the experiment) indexed by $t=1, \ldots, 5$ and in two treatment groups (early and late charges).

Denote $P_{i t}^{A}\left(\theta, p_{i t}\right)$ the probability to take the detour route (not intersect the congestion area) in time period $t$ when pricing is $p_{i t}$. In the data, define $\widetilde{P}_{i t}^{A}$ the fraction of days when commuter home-work trips do not intersect the congestion area for individual $i$, which depends on $i$ 's treatment group. For $t=1, \ldots, 5$, the route moments are:

$$
\begin{aligned}
& g_{i}^{49+t}\left(\theta, p_{i t}\right)=T_{i}^{\text {Early }} \cdot\left[\widetilde{P}_{i t}^{A}-P_{i t}^{A}\left(\theta, p_{i t}\right)\right] \\
& g_{i}^{54+t}\left(\theta, p_{i t}\right)=\left(1-T_{i}^{\text {Early }}\right) \cdot\left[\widetilde{P}_{i t}^{A}-P_{i t}^{A}\left(\theta, p_{i t}\right)\right] .
\end{aligned}
$$

## A. 5 Parameter Sensitivity Measure

Table A 3 reports the estimated sensitivity measure $\Lambda$ from Andrews et al. (2017), scaled by the standard deviation of each moment. Each entry $\Lambda_{p j}$ measures the change in estimated parameter $\theta_{p}$ due to a one standard deviation change in moment $m_{j}$. The measure is $\hat{\Lambda}=\left(\hat{S}^{\prime} \hat{W} \hat{S}\right)^{-1} \hat{S}^{\prime} \hat{W} \operatorname{diag}(\hat{\sigma})$ where $\hat{S}$ is the Jacobian evaluated at the estimated parameters, $\hat{W}$ is the optimal weighting matrix, and $\hat{\sigma}$ is the vector of bootstrap standard deviation of moment $j$.

## A. 6 Road Technology Invariance Result

Conditional on the relationship (8) estimated on a representative sample, the impact of an additional trip on total driving time in Bangalore is invariant to the aggregate volume of traffic in Banglore, and it is invariant to the sample size used to estimate the road technology relationship.

The key intuition is that equation (8) depends on normalized density, so it is invariant to the true aggregate volume of traffic. Then, imagine that the aggregate volume is twice as large as initially believed. Then the impact of a single trip on travel delay will be twice as small. However, it will affect twice as many other commuters, so the impact on total time is not affected.

Using the notation from section 4.3 let $Q=(q(h, K))_{h, k}$ denote the pattern of departures, where $q(h, K)$ is the mass of trips of length $K$ starting at $h$, based on a sample of $N$ trips. Let $x=(x(h))_{h}$ denote the instantaneous travel delay profile, and $d=(d(h))_{h}$ the density profile. Similar to equation (8), assume that instantaneous delay satisfies $x(h)=\lambda_{0}+\lambda_{1} d(h) / N$ where $N$ is the number of trips in the sample.

Proposition 4. The marginal effect of an additional trip on total travel time does not depend on the sample size used to construct $Q$.

Proof. Let $d\left(h^{\prime}, Q\right)$ denote density at time $h^{\prime}$ as a function of the pattern of departures, and $d(Q)=$ $\left(d\left(h^{\prime}, Q\right)\right)_{h^{\prime}}$.

Travel times are uniquely determined by the instantaneous travel delay profile, which depends on normalized density. Hence, we can write average travel times as a function $\bar{T}\left(\frac{d(Q)}{N}\right)$. Note that total travel time in the city is $N \bar{T}$.

For every $h^{\prime}, d\left(h^{\prime}, Q\right)$ is homogeneous of degree 1 in $Q$. Consequently, the partial derivative $d_{h, K}\left(h^{\prime}, Q\right)$ with respect to the mass of trips with length $K$ starting at $h$ is degree 0 in $Q$, i.e. it does not depend on the sample size used to compute $Q$.

Consider adding a trip of length $K$ that starts at $h$ and denote the pattern of departures by $Q+\mathbf{1}(h, K)$. The change in total travel time is

$$
N\left(\bar{T}\left(\frac{d(Q+\mathbf{1}(h, K))}{N}\right)-\bar{T}\left(\frac{d(Q)}{N}\right)\right) \approx N \frac{\partial \bar{T}}{\partial \mathbf{1}(h, K)}=N \sum_{h^{\prime}} \frac{\partial \bar{T}}{\partial h^{\prime}} \frac{d_{h, K}\left(h^{\prime}, Q\right)}{N}
$$

The last term does not depend on $N$ because neither $\frac{\partial \bar{T}}{\partial h^{\prime}}$ nor $d_{h, K}\left(h^{\prime}, Q\right)$ depend on $N$.

## A. 7 Policy Simulations

For policy simulations I use a 5 -minute departure time grid from 5 am to 2 pm . Each simulation has 3040 agents, with each real study participant replicated with 10 independent random draws of ideal arrival times from the distribution recovered with non-negative least squares (section 7.3). The vector of ideal arrival times is re-sampled during bootstrapping. Thus, the confidence intervals include uncertainty due to numerical simulation. Benchmark results are robust to using $10 \times$ more agents.

For the two-route equilibrium model, I assume double the volume of trips, so that on average the volume of trips per route remains the same.

I use a nested logit model for the equilibrium model with an extensive margin decision. The outer nest has two options, taking the trip $(z=1)$ and not taking the trip $(z=0)$. Trips are valuable: a commuter not making a trip incurs a cost proportional to trip length $\omega_{i}=\omega \cdot \mathrm{K}_{i} / \overline{\mathrm{K}}$. Expected utility is given by:

$$
\mathrm{E} u_{i}\left(x, h, h_{i}^{A}\right)= \begin{cases}\mathrm{E} v\left(h, \mathcal{T}_{i}(h), h_{i t}^{A}\right)-p_{i t}(h)+\varepsilon_{i t}(1, h) & z=1  \tag{11}\\ -\omega_{i}+\varepsilon_{i}(0, h) & z=0\end{cases}
$$

where $\varepsilon_{i}(z, h)$ follow a type-1 extreme value distribution with correlation within each value of $z$, with logit scale parameter $\eta$ for the trip (upper) nest.

The congestion pricing experiment was not designed to estimate the extensive margin trip elasticity.

## A. 8 Online Appendix: Figures

Figure A1: Impact of Departure Time Charges on Departure Times (Commuting Trips)


Panel (A) Morning Peak


Panel (B) Evening Peak

Notes: Version of Figure 2 restricting to regular commuters and trips between home and work (both ways).

Figure A2: Travel Demand Model Fit


Panel (A) Departure Time Difference in Differences


Panel (B) Departure Time Control Post


Notes: This figure shows in- an out-of-sample fit for the estimated travel demand model. Panel A plots the departure time moments that correspond to the difference-in-differences (treated vs. control, during vs. before), the analogue of Figure A1 Panel B shows the probability density of departure time in the control group during the experiment (Post). These moments are not directly targeted in the estimation (however, the ideal departure time distribution inversion routine depends on the distribution of departure time before the experiment). Panel C shows the dynamic route choice moments, the analogue of Figure 3 . Panel D shows detour route choice heterogeneity by the amount of detour (in minutes), for the "early" treatment group, which receives charges in week 1. This is the analogue of Figure SM4 and these moments are not targeted in estimation. For all graphs, the model is indicated by thicker, red lines.

Figure A3: Travel Demand Model: Understanding Identification


Panel (A) Jacobian: $d$ moment $/ d$ parameter


Panel (B) Sensitivity: $d$ parameter $/ d$ moment Notes: Moments are defined as $g_{j}(\theta)=s_{j}(\theta)-s_{j, \text { data }}$. Panel A plots the partial derivatives $d g(h, \theta) / d \beta_{E}$ and $d g(h, \theta) / d \beta_{L}$ for each departure time moment $g(h, \theta)$. Panel B plots the scaled sensitivity measure from Andrews et al. 2017, quantifying the change in the estimated early and late schedule cost parameters $\widehat{\beta}_{E}$ and $\widehat{\beta}_{L}$ given by one standard deviation change in each of the 49 departure time moments, as well as the LOESS fit. See Appendix A.5 for definitions.

Figure A4: Travel Demand Model Numerical Identification Check and Finite Sample Properties


Schedule Cost Early $\beta_{E}$
Schedule Cost Late $\beta_{L}$






Notes: This figure compares true random parameters and the estimated parameters from simulated data, under two scenarios. In the "asymptotic" scenario (red circles) the simulated data has exact (route and departure time) choice probabilities. In the "finite sample" scenario (blue triangles) the simulated data has random choices and I use exactly the same data set size as in the real data (the number of observations per commuter). Simulations are based on 100 random parameters independently drawn between $25 \%$ and $175 \%$ of the benchmark estimated values. For each set of parameters, I first invert the $f_{i}^{A}$ distributions from pre-experiment (real) data, then use it to simulate data. I then estimate the model on the simulated data using one random starting condition that is independent of the parameters used to simulate the model. Each graph shows the estimated parameter on the Y axis, and the true parameter on the X axis. Outlier values are censored. The diagonal line is identity. See also Table A12.

Figure A5: Road Technology Estimation Robustness Checks


Panel (A) Travel Delay from GPS Data and Google Maps


Panel (C) Recruitment Time and Trip Time Distributions


Panel (E) Peak-hour Use of Lower Externality Routes


Panel (B) Travel Delay and Traffic Volume


Panel (D) Comparison with Akbar and Duranton, 2017)

Notes: Panel A uses travel delay from GPS trips to replicate Figure 4 including percentiles. See Table SM10 notes. Panel B replicates Figure 4 with "volume," the normalized number of trips starting each hour on the X axis. Panel C plots the distribution of participant recruitment times (histogram in solid gray) and the distribution of trip departure times (kernel density plot in solid blue line). Both Y axes start at zero. Panel D compares log-log road technology estimates from this paper (gray dots, dashed blue line) with those from Akbar and Duranton (2017) in Bogotá (red solid line). (Their estimate is computed from Figure 4 panel C.) Panel E describes peak-hour substitution towards routes with less steep travel time profiles. For each commuter in the experimental sample, I query from Google Maps the entire travel time profile for every route that is optimal at some departure time. For each route I compute its slope, the change in travel delay between 6:30 and 9:30 am. The right axis (black dashed line) plots the fraction of commuters for whom their highest slope route is fastest at departure time $h$. The left axis (blue solid line) plots the average slope of the optimal route at $h$.

Figure A6: Road Technology at the Daily Level


Notes. These graphs replicate Figure 4 panel A by date. The first 7 panels show the relationship between hourly GPS traffic volume and Google Maps travel delay for 7 randomly chosen calendar dates (one for each day of the week). The last panel overlays the predicted fit for all calendar dates in the sample. The sample is calendar dates with above-median number of GPS trips (at least 571 trips per day). Travel delay and traffic density at the day $d$ and hour $h$ level correspond to column 3 in Table 3. Each fit is a power fit as in column 2 in Table 3.

Figure A7: Road Technology on Major Arteries


Notes. These graphs replicate Figure 4 for major arteries depicted in Figure SM1, separately by direction. The Y axis is average Google Maps travel delay for that road segment. To compute traffic density at the artery level, I define a buffer area around each artery. I then count the number of GPS trips that travel along the artery in each direction for each time of day, excluding short trips that intersect the artery for less than 200 meters (which I assume correspond to cross-traffic). I obtain 268,292 trip segments on the 46 arteries. $95 \%$ confidence intervals based on Newey-West standard errors with a 3 -hour lag also reported.

Figure A8: Policy Counterfactual Additional Results


Panel (A) Optimal Congestion Charges


Panel (C) Non-linear Road Technologies


Panel (B) Departure Volume


Panel (D) Varying the Total Volume of Trips

Notes. Panel A plots percentiles of the optimal charges (equal to marginal social cost) around the social optimum. For comparison, I plot the average trip delay (red, solid line) as in Figure 5 and the instantaneous travel delay (blue, dashed line). Panel B plots the rates of trip departure rates in the Nash equilibrium and in the social optimum. Panel C overlays the alternate road technologies used in panel D of Table 4, over the benchmark road technology (Figure 4). I use the estimated $\lambda_{0}$ and $\lambda_{1}$ from the benchmark linear equation 8 and only vary $\nu$. Panel D shows equilibrium peak average travel delay ( X axis) and welfare gain from optimal pricing (Y axis) when varying the total volume of trips used in the simulation.

Figure A9: Decomposing Gains and Losses in the Social Optimum


Panel (A) Real Changes: Travel Time and Schedule Costs


Panel (B) Net of Charges and Rebates

Notes. For each commuter and ideal arrival time $h_{i}^{A}$, the X axis is the average departure time $h_{i}=\mathrm{E} h\left(h_{i}^{A}\right)$ in Nash. Panel A plots the Nash-social optimum difference in -E $\alpha T\left(h_{i}\right)$ vs $h_{i}$ (black, solid line) and in $-\mathrm{E} \beta_{E}\left|h_{i}+T\left(h_{i}\right)-h_{i}^{A}\right|_{-}+\beta_{L}\left|h_{i}+T\left(h_{i}\right)-h_{i}^{A}\right|_{+}$vs $h_{i}$ (green, dashed line). Panel B plots average expected utility change vs $h_{i}$ when commuters receive a rebate that is proportional to trip length (black, solid line) or constant (green, dashed line).

Figure A10: Policy Counterfactual in Two Route Equilibrium Model


Panel (A) Road Technology for Two Routes


Panel (C) Average Travel Delay by Route


Panel (B) Steeper Route Choice Probability

Notes: This Figure describes the two-route equilibrium (panel E of Table 4). Panel A overlays the alternate highexternality route road technologies over the benchmark road technology (Figure 4). Panel B plots the probability of taking the high-externality route by departure time, in the Nash equilibrium and in the social optimum, in the tworoute model where one route has $15 \%$ higher slope. Panel C replicates Figure 5 by route for the two-route model where one route has $15 \%$ higher slope.

## A. 9 Online Appendix: Tables

Table A1: Descriptive Statistics about Travel Behavior

| Panel A. Trip Characteristics |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Median | Mean | Std. Dev. | 10 Perc. | 90 Perc. | Obs. |
| Total Number of Trips |  |  |  |  |  | 51,473 |
| Number of Trips per Day | 2.86 | 3.15 | $[1.16]$ | 1.90 | 4.86 | 497 |
| Median trip duration (minutes) | 24.50 | 27.43 | $[12.83]$ | 15.20 | 42.60 | 497 |
| Median trip length (Km.) | 5.91 | 7.17 | $[4.67]$ | 2.92 | 13.36 | 497 |
| Panel B. Commute Destination Variability |  |  |  |  |  |  |
| Regular Commuter |  |  |  |  |  |  |
| Frac. trips Home-Work, Work-Home | 0.38 | 0.39 | $[0.21]$ | 0.13 | 0.67 | 378 |
| Frac. of trips Work-Work | 0.03 | 0.06 | $[0.08]$ | 0.00 | 0.15 | 378 |
| Frac. of days present at Work | 0.92 | 0.86 | $[0.16]$ | 0.60 | 1.00 | 378 |
| Panel C. Departure Time Variability |  |  |  |  |  |  |
| (Standard Deviation of the Departure | Time in hours) |  |  |  |  |  |
| First Trip (AM) |  |  |  |  |  |  |
| Last Trip (PM) | 1.28 | 1.24 | $[0.50]$ | 0.54 | 1.83 | 496 |
| First Home to Work Trip (AM) | 1.72 | 1.71 | $[0.50]$ | 1.04 | 2.36 | 497 |
| Last Work to Home Trip (PM) | 0.48 | 0.62 | $[0.52]$ | 0.15 | 1.28 | 332 |

Notes: This table reports summary travel behavior statistics for the experimental sample of 497 commuters. See section 5.1 for the definition of home and work locations and of regular commuter. In panel C, I compute the within-commuter variation in departure times for different classes of trips.

Table A2: Experimental Design
Panel A. Treatment Strata

|  |  |  | Departure Time <br> Sub-treatment |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :---: |
| Route <br> Eligibility | Car or <br> Moto | Daily KM | High <br> Rate | Low <br> Rate | Info | Control |  |
| Eligible | Car | Low | $3 / 8$ | $1 / 8$ | $2 / 8$ | $2 / 8$ |  |
| Eligible | Car | High | $1 / 8$ | $3 / 8$ | $2 / 8$ | $2 / 8$ |  |
| Eligible | Moto | Low | $3 / 8$ | $1 / 8$ | $2 / 8$ | $2 / 8$ |  |
| Eligible | Moto | High | $1 / 8$ | $3 / 8$ | $2 / 8$ | $2 / 8$ |  |
| Ineligible | Car | Low | $1 / 12$ | $3 / 12$ | $4 / 12$ | $4 / 12$ |  |
| Ineligible | Car | High | $3 / 12$ | $1 / 12$ | $4 / 12$ | $4 / 12$ |  |
| Ineligible | Moto | Low | $1 / 12$ | $3 / 12$ | $4 / 12$ | $4 / 12$ |  |
| Ineligible | Moto | High | $3 / 12$ | $1 / 12$ | $4 / 12$ | $4 / 12$ |  |

Panel B. Treatment Timing

|  |  |  | Treatment by <br> Route <br> Eligibility |  |  |  |
| :---: | :---: | :--- | :---: | :---: | :---: | :---: |
|  | Dep. Time <br> Timing | Dep. Time <br> Sub-Treatment | Experiment |  |  |  |

Notes. There were eight strata in the experiment, all combinations of participants eligible or ineligible for the route charge, car or non-car (motorcycle or scooter) users, and participants with high or low daily travel distance in the baseline period. Departure time sub-treatment probabilities are given in panel A. There are eight route sub-treatments: all combinations of high/low charges, short/long detour, and early/late. All have equal probabilities. Sub-treatment are cross-randomized (see section SM.6). Treatment timing is presented in panel B. The letter R corresponds to the route treatment. The letters H, L, I and C respectively correspond to high-rate, low-rate, information and control in the departure time treatment.

Table A3: Experimental Participant Sample Representativeness


Notes. These results describe respondent selection into experiment by comparing the experimental sample (497 respondents) to the entire sample of eligible commuters approached in gas stations by the survey team (panel A) and to the full survey sample (panels B and C). The sample in Panel A is all respondents approached in gas stations, excluding ineligible respondents. Weights are used to (a) account for missing data for each variable, and (b) to adjust for the estimated $\sim 52 \%$ ineligible respondents among survey refusals (for refusals, 7,218 respondents did not complete the eligibility filter, and I assume the same proportion were ineligible). Gender, age and car driver variables are visually assessed by the surveyor for all respondents. Vehicle value (residual) is imputed based on vehicle type (car/motorcycle), make and model, using pricing data scrapped from a used-vehicles website in Bangalore, residualized on a "car" dummy. Monthly income is self-reported during the recruitment survey (the respondent is handed the tablet to enter the amount confidentially - the surveyor never sees the amount), truncated at 100, 000 INR ( $\sim 1,300$ USD). Occupation is self-reported during the recruitment survey. Value of time and schedule flexibility are based on choices in hypothetical scenarios in a follow-up phone survey; see section SM.4.2 for details. The difference in SD units includes significance levels from a (weighted) regression of the row outcome variable on an indicator for being in the experiment. ${ }^{*} p \leq 0.10,{ }^{* *} p \leq 0.05,{ }^{* * *} p \leq 0.01$

Table A4: Experimental Balance Checks

|  |  | Departure Time Treatments |  |  |  |  |  |  |  | Route Treatment |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Information |  | Low Rate |  | High Rate |  | Obs. | Control <br> Mean | Route Early | (S.E.) |  | Control <br> Mean |
|  |  |  | (S.E.) |  | (S.E.) |  | (S.E.) |  |  |  |  |  |  |
| (1) | Car user | 0.01 | (0.02) | 0.01 | (0.01) | 0.01 | (0.02) | 497 | 0.28 | -0.01 | (0.01) | 254 | 0.28 |
| (2) | Regular destination | -0.05 | (0.05) | 0.00 | (0.05) | -0.09* | (0.05) | 497 | 0.77 | -0.05 | (0.03) | 254 | 0.95 |
| (3) | Age | -0.93 | (0.93) | 1.26 | (1.01) | -0.09 | (1.07) | 497 | 33.20 | -1.35 | (0.94) | 254 | 34.30 |
| (4) | Log vehicle price | 0.11** | (0.05) | 0.09 | (0.05) | 0.03 | (0.06) | 453 | 11.06 | 0.00 | (0.05) | 231 | 11.17 |
| (5) | Log income | 0.01 | (0.10) | -0.02 | (0.14) | -0.07 | (0.14) | 411 | 10.11 | -0.09 | (0.12) | 211 | 10.24 |
| (6) | Frac days with good GPS data | -0.01 | (0.03) | -0.02 | (0.03) | -0.00 | (0.03) | 497 | 0.41 | 0.00 | (0.03) | 254 | 0.42 |
| (7) | Frac days present at work | 0.01 | (0.03) | 0.00 | (0.03) | -0.03 | (0.04) | 497 | 0.70 | -0.03 | (0.03) | 254 | 0.79 |
| (8) | Number of trips per day | -0.12 | (0.11) | -0.05 | (0.13) | -0.00 | (0.14) | 497 | 1.25 | -0.00 | (0.12) | 254 | 1.15 |
| (9) | Total distance per day (Km.) | -0.46 | (0.69) | -0.22 | (0.83) | 0.32 | (0.88) | 497 | 8.29 | 0.19 | (0.83) | 254 | 8.79 |
| (10) | Total duration per day (min) | -2.99 | (3.04) | -1.51 | (3.55) | 1.23 | (3.84) | 497 | 35.52 | 0.49 | (3.50) | 254 | 35.49 |
| (11) | Total D.T. hypothetical rate per day | -0.84 | (3.82) | -0.83 | (3.90) | -0.32 | (4.20) | 497 | 38.82 | -0.51 | (3.79) | 254 | 37.92 |
| (12) | Total Route hypothetical rate per day | -2.27 | (3.18) | -2.85 | (4.23) | -0.40 | (4.88) | 497 | 23.83 | 0.69 | (5.61) | 254 | 50.73 |
| (13) | Joint Significance Test F-stat | $0.26$ |  |  |  |  |  |  |  | $0.02$ |  |  |  |
| $(14)$ | Joint Significance Test P-value | $0.86$ |  |  |  |  |  |  |  | 0.90 |  |  |  |

Notes. This table shows experimental balance checks for the departure time and route treatments. Variables 1,3,4, and 5 are from the recruitment survey, while the remaining eight variables are calculated from the GPS trips data before the experiment. Each row and group of columns combination reports coefficients from a regressions with the row header as outcome. In the "Route Treatment" columns, the sample is restricted to 254 participants who receive the route treatment, and the dependent variable is whether the respondent was assigned to the "early" route sub-treatment (to receive the route charges in week 1 as opposed to week 4). All regressions include randomization strata dummies. Rows 13 and 14 report the F-statistic and p-value from column-wise joint significance tests. Robust standard errors are shown in parentheses. ${ }^{*} p \leq 0.10,{ }^{* *} p \leq 0.05,{ }^{* * *} p \leq 0.01$

Table A5: GPS Data Quality at Daily Level (Attrition Check)

|  | $(1)$ | $(2)$ |
| :--- | :---: | :---: |
| Treatment | Departure Time | Route |
| Commuter FE | X | X |
|  |  |  |
| High Rate $\times$ Post | 0.02 |  |
|  | $(0.05)$ |  |
| Low Rate $\times$ Post | -0.00 |  |
|  | $(0.05)$ |  |
| Information $\times$ Post | -0.00 |  |
|  | $(0.04)$ | 0.02 |
| Route Charges |  | $(0.04)$ |
|  |  | $0.14^{* * *}$ |
| Post | $0.08^{* *}$ | $(0.04)$ |
|  | $(0.03)$ | 9,809 |
| Observations | 24,779 | 0.76 |
| Control Mean | 0.76 |  |

Notes. This table shows experimental impacts on the quality of the GPS data received from study participants. The outcome is a dummy for good quality GPS data on a given day (see section SM.3). The sample covers all non-holiday weekdays for all experiment participants, excluding days outside Bangalore. In the post period, the sample in column 1 is restricted to the departure time treatment period, either the first or the last three weeks. The sample in column 2 is restricted to the first week in the experiment. All specifications include respondent and study cycle fixed effects. Standard errors are clustered at the respondent level. ${ }^{*} p \leq 0.10,{ }^{* *} p \leq 0.05,{ }^{* * *} p \leq 0.01$

Table A6: Impact of Departure Time Charges on Daily Total Hypothetical Rate: Commuting Trips

| Time of Day | (1) <br> AM \& PM | (2) | (3) | (4) | (5) | (6) | (7) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | AM |  |  | PM |  |  |
|  |  | all | pre peak | post <br> peak | all | pre <br> peak | post <br> peak |
| Commuter FE | X | X | X | X | X | X | X |
| Sample: | Regular Commuters, Home-Work and Work-Home Trips |  |  |  |  |  |  |
| Charges $\times$ Post | $\begin{gathered} -7.94^{* * *} \\ (2.89) \end{gathered}$ | $\begin{gathered} -3.76^{* *} \\ (1.90) \end{gathered}$ | $\begin{gathered} -3.00^{*} \\ (1.56) \end{gathered}$ | $\begin{gathered} -0.76 \\ (1.20) \end{gathered}$ | $\begin{gathered} -4.18^{* *} \\ (1.67) \end{gathered}$ | $\begin{gathered} -0.88 \\ (1.23) \end{gathered}$ | $\begin{gathered} -3.30^{* * *} \\ (1.08) \end{gathered}$ |
| Post | $\begin{gathered} -1.74 \\ (2.65) \end{gathered}$ | $\begin{gathered} -0.74 \\ (1.74) \end{gathered}$ | $\begin{aligned} & -1.29 \\ & (1.30) \end{aligned}$ | $\begin{gathered} 0.55 \\ (1.36) \end{gathered}$ | $\begin{gathered} -1.00 \\ (1.61) \end{gathered}$ | $\begin{gathered} -0.69 \\ (1.18) \end{gathered}$ | $\begin{gathered} -0.31 \\ (1.06) \end{gathered}$ |
| Observations | 12,115 | 12,115 | 12,115 | 12,115 | 12,115 | 12,115 | 12,115 |
| Control Mean | 40.80 | 23.37 | 14.27 | 9.10 | 17.44 | 9.15 | 8.29 |

Notes: This table reports the impact of departure time charges on daily total hypothetical rates for regular commuters and commuting trips, separately by time interval. The sample of users and days, and the specifications, are the same as in Table 1 panel B, further restricted to regular commuters and direct trips between their home and work locations (in either direction). Columns (3) and (6) restrict to trips before the peak, i.e. the mid-point of the rate profile. Columns (4) and (7) restrict to trips after the peak. Table SM3 reports these results for variable commuters. Standard errors in parentheses are clustered at the respondent level. ${ }^{*} p \leq 0.10,{ }^{* *} p \leq 0.05,{ }^{* * *} p \leq 0.01$

Table A7: Impact of Route Charges on Detour Route Usage

|  | (1) | (2) | (3) | (4) |
| :---: | :---: | :---: | :---: | :---: |
| Outcome | Use Detour Route |  | Number of Trips Today |  |
| Commuter FE | X | X | X | X |
| Panel A. All Commuters |  |  |  |  |
| Treatment: Early $\times$ week 1 | $\begin{gathered} 0.27^{* * *} \\ (0.05) \end{gathered}$ | $\begin{gathered} 0.26^{* * *} \\ (0.05) \end{gathered}$ | $\begin{gathered} 0.02 \\ (0.07) \end{gathered}$ | $\begin{gathered} 0.02 \\ (0.07) \end{gathered}$ |
| Persistence: Early $\times$ week 2 |  | $\begin{gathered} 0.09^{* *} \\ (0.04) \end{gathered}$ |  | $\begin{gathered} -0.09 \\ (0.08) \end{gathered}$ |
| Observations | 5,235 | 6,038 | 9,809 | 11,016 |
| Control Mean (week 1) | 0.11 | 0.11 | 0.73 | 0.73 |
| Panel B. Commuters Who Used Detour at Baseline |  |  |  |  |
| Treatment: Early $\times$ week 1 | $\begin{gathered} 0.41^{* * *} \\ (0.08) \end{gathered}$ | $\begin{gathered} 0.41^{* * *} \\ (0.08) \end{gathered}$ | $\begin{gathered} 0.03 \\ (0.13) \end{gathered}$ | $\begin{gathered} 0.02 \\ (0.13) \end{gathered}$ |
| Persistence: Early $\times$ week 2 |  | $\begin{aligned} & 0.13^{*} \\ & (0.07) \end{aligned}$ |  | $\begin{gathered} -0.01 \\ (0.13) \end{gathered}$ |
| Observations | 2,369 | 2,718 | 3,508 | 3,940 |
| Control Mean (week 1) | 0.18 | 0.18 | 0.87 | 0.87 |

Notes: This table reports difference-in-differences impacts of the route treatment on trip and daily outcomes. In the first two columns, an observation is a commuting trip between home and work, and the outcome is whether the commuting trip used a detour route (defined as any route that avoids the congestion area). The last two columns, an observation is a commuter, day combination, and the outcome is the total number of trips that day. The sample is all non-holiday weekdays with good quality GPS data, excluding days outside Bangalore. In the post period, all days except trial days are included. The sample is restricted to 243 participants in the route treatment. In the first two columns, only frequent commuters are included. In panel B, the sample is restricted to commuters who used a detour route between home and work at least once before the experiment. All specifications include respondent and study cycle fixed effects. The mean of the outcome variable in the control (late) group in week 1 of the experiment is reported for each specification. Standard errors in parentheses are clustered at the respondent level. ${ }^{*} p \leq 0.10,{ }^{* *} p \leq 0.05,{ }^{* * *} p \leq 0.01$

Table A8: Impact of Route Charge Sub-Treatments on Daily Outcomes

|  | Hypothetical Route Charges |  |
| :--- | :---: | :---: |
|  | $(1)$ | $(2)$ |
| Treated $\times$ High Rate | $-41.1^{* * *}$ |  |
| Treated $\times$ Low Rate | $(13.1)$ |  |
|  | -21.5 |  |
| Treated $\times$ Short Detour | $(13.3)$ | $-43.0^{* * *}$ |
|  |  | $(15.4)$ |
| Treated $\times$ Long Detour |  | -26.2 |
|  |  | $(17.8)$ |
| Observations | 6,129 | 3,693 |
| Commuters | 243 | 148 |
| Control Mean | 117.1 | 122.7 |
| P-val Equal Sub-treatment Effects | 0.30 | 0.48 |

Notes: This table reports difference-in-differences impacts of route sub-treatments on daily total hypothetical route charges. The sample in column 1 is the same as in Table A7 covering the period before and during the first week in the experiment. In column 2 the sample is restricted to 148 route treatment participants for whom candidate areas included at least one with short detour (3-7 minutes) and at least one with long detour ( $7-14$ minutes). The outcome is total daily hypothetical route charges; higher values indicate lower detour usage. Standard errors in parentheses are clustered at the respondent level. ${ }^{*} p \leq 0.10,{ }^{* *} p \leq 0.05$, ${ }^{* * *} p \leq 0.01$

Table A9: Travel Demand Estimates: Additional Results

|  | $(1)$ | $(2)$ | $(3)$ | $(4)$ | $(5)$ <br> Parameters <br> prop. to <br> wage | Single ideal <br> arrival time |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Static <br> Route Choice | Asymmetric <br> switching cost | Time FE | Half <br> attention |  |  |
| $\beta_{E}$ : Schedule cost early (INR/hour) | 659 | 570 | 489 | 307 | 423 | 1267 |
|  | $[432,1359]$ | $[333,1450]$ | $[262,1122]$ | $[201,1581]$ | $[212,3138]$ | $[372,22567]$ |

Notes: Column 1 fits a model with static route choice ( $\delta=\gamma=0$ ) using only two route choice moments: the fraction using route 1 when not charged during the experiment, and when charged. Column 2 modifies the benchmark model to include asymmetric switching costs parametrized by $\gamma_{01}=\gamma_{10}=2 \gamma$. Column 3 estimates time fixed effects $\eta_{1}, \eta_{2}, \eta_{3}, \eta_{4}$ that enter route 1 utility on the corresponding weeks during the experiment. Column 4 imposes that each commuter ignores experimental congestion charges with independent probability $p=0.5$. In column 5 , all preference parameters are proportional to $w_{i}$, commuter $i$ 's self-reported hourly wage. (Note that logit parameters are proportional to $w_{i}$ and to normalized trip length, i.e. $\sigma_{i}^{D T}=\sigma \frac{w_{i}}{\bar{w}} \frac{K_{i}}{\bar{K}}$ ). In column 6 , I assume that all commuters have the same ideal arrival time that does not vary over time, $h_{i t}^{A}=h^{A}$.

Table A10: Travel Demand Estimation: Discount Factor Robustness

|  | (1) | (2) | (3) | (4) | (5) |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Varying Discount Factor $\delta$ |  |  |  | Estimate $\delta$ |
| $\beta_{E}$ : Schedule cost early (INR/hour) | $\begin{gathered} 570 \\ {[299,1358]} \end{gathered}$ | $\begin{gathered} 509 \\ {[294,1062]} \end{gathered}$ | $\begin{gathered} 552 \\ {[301,1539]} \end{gathered}$ | $\begin{gathered} 553 \\ {[307,1156]} \end{gathered}$ | $\begin{gathered} 548 \\ {[270,1375]} \end{gathered}$ |
| $\beta_{L}$ : Schedule cost late (INR/hour) | $\begin{gathered} 381 \\ {[200,613]} \end{gathered}$ | $\begin{gathered} 367 \\ {[254,2119]} \end{gathered}$ | $\begin{gathered} 344 \\ {[245,1262]} \end{gathered}$ | $\begin{gathered} 352 \\ {[244,1317]} \end{gathered}$ | $\begin{gathered} 350 \\ {[244,1450]} \end{gathered}$ |
| $\alpha$ : Value of travel time (INR/hour) | $\begin{gathered} 1180 \\ {[549,1501]} \end{gathered}$ | $\begin{gathered} 709 \\ {[323,1142]} \end{gathered}$ | $\begin{gathered} 609 \\ {[365,1210]} \end{gathered}$ | $\begin{gathered} 594 \\ {[390,1252]} \end{gathered}$ | $\begin{gathered} 624 \\ {[234,1048]} \end{gathered}$ |
| $\gamma$ : Route switching cost (INR) | $\begin{gathered} 78.4 \\ {[58.6,122.9]} \end{gathered}$ | $\begin{gathered} 89.2 \\ {[55.4,114.9]} \end{gathered}$ | $\begin{gathered} 80.3 \\ {[43.2,112.2]} \end{gathered}$ | $\begin{gathered} 87.0 \\ {[44.1,114.7]} \end{gathered}$ | $\begin{gathered} 79.7 \\ {[62.9,121.6]} \end{gathered}$ |
| $\sigma^{D T}:$ Logit departure time | $\begin{gathered} 22.5 \\ {[1.8,78.5]} \end{gathered}$ | $\begin{gathered} 21.4 \\ {[1.1,73.9]} \end{gathered}$ | $\begin{gathered} 19.5 \\ {[1.3,68.0]} \end{gathered}$ | $\begin{gathered} 20.4 \\ {[1.9,74.3]} \end{gathered}$ | $\begin{gathered} 20.6 \\ {[1.4,82.3]} \end{gathered}$ |
| $\sigma^{R}$ : Logit route (upper nest) | $\begin{gathered} 62.0 \\ {[34.2,63.6]} \end{gathered}$ | $\begin{gathered} 57.6 \\ {[37.9,64.6]} \end{gathered}$ | $\begin{gathered} 57.9 \\ {[41.8,76.4]} \end{gathered}$ | $\begin{gathered} 50.6 \\ {[34.1,67.7]} \end{gathered}$ | $\begin{gathered} 58.6 \\ {[40.1,68.5]} \end{gathered}$ |
| $\delta$ : discount factor | 0.00 | 0.50 | 0.90 | 0.99 | $\begin{gathered} 0.88 \\ {[0.36,0.98]} \end{gathered}$ |
| Model: |  |  |  |  |  |
| Dynamic route choice model | Dynamic | Dynamic | Dynamic | Dynamic | Dynamic |
| Fixed discount factor ( $\delta$ ) | 0.0 | 0.50 | 0.90 | 0.99 | - |
| Moments: |  |  |  |  |  |
| Dynamic route choice (10) | Yes | Yes | Yes | Yes | Yes |
| Route choice transition (1) | - | - | - | - | Yes |

Notes: Columns 1-4 replicate column 1 in Table 2 with different assumptions on $\delta$. In column 5 I estimate $\delta$, using an additional moment. This moment measures the transition probability between route 0 and route 1 , on average, between weeks 1-2, 2-3, and 3-4 during the experiment. In the data, I define that the commuter uses route 0 if the average weekly route choice of route 0 is strictly below 0.5 .

Table A11: Dynamic Route Choice Model Identification


Notes: This table reports the Jacobian matrix for three moments with respect to three route choice parameters (VOTT $\alpha$, switch cost $\gamma$ and logit scale $\sigma^{R}$ ). The three moments are the route treatment "early" group average detour route usage (1) before the experiment, (2) during week 1 in the experiment (when charges were in effect), and (3) in week 2 (after charges had ended). The first group of columns uses the benchmark model, and the next group uses the dynamic route choice model without departure time (column 4 in Table 22. In the last group of columns, I estimate a simple model where a single agent faces the average detour (6.4 minutes) and the average route charge (144 INR), and I assume $\delta=0$ (see Appendix A.2). Jacobian entries are divided by the value of the parameter, so they represent the semi-elasticity of the moment with respect to a proportional change in the parameter.

Table A12: Travel Demand Model Finite Sample Properties Check

|  | $(1)$ | $(2)$ | $(3)$ | $(4)$ | $(5)$ | $(6)$ |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Estimated Parameter |  |  |  |  |  |  |  |  |
| (True) Value of time $\alpha$ | $\widehat{\alpha}$ | $\widehat{\beta}_{E}$ | $\widehat{\beta}_{L}$ | $\widehat{\gamma}$ | $\widehat{\sigma^{D T}}$ | $\widehat{\sigma^{R}}$ |  |  |  |  |  |
|  | $1.09^{* * *}$ | $0.15^{* * *}$ | 0.04 | $-0.01^{*}$ | 0.00 | $-0.00^{* *}$ |  |  |  |  |  |
| (True) Penalty early $\beta_{E}$ | $(0.07)$ | $(0.06)$ | $(0.04)$ | $(0.00)$ | $(0.00)$ | $(0.00)$ |  |  |  |  |  |
|  | 0.01 | $0.55^{* * *}$ | 0.03 | -0.00 | -0.00 | $0.00^{*}$ |  |  |  |  |  |
| (True) Penalty late $\beta_{L}$ | $(0.06)$ | $(0.07)$ | $(0.04)$ | $(0.01)$ | $(0.01)$ | $(0.00)$ |  |  |  |  |  |
|  | -0.08 | 0.12 | $0.90^{* * *}$ | 0.00 | -0.01 | 0.00 |  |  |  |  |  |
| (True) Switch Cost $\gamma$ | $(0.09)$ | $(0.07)$ | $(0.12)$ | $(0.01)$ | $(0.01)$ | $(0.00)$ |  |  |  |  |  |
|  | 0.53 | 0.60 | 0.47 | $0.90^{* * *}$ | -0.02 | -0.02 |  |  |  |  |  |
| (True) Logit departure time $\sigma^{D T}$ | -0.23 | -1.42 | 0.37 | 0.00 | $0.81^{* * *}$ | -0.00 |  |  |  |  |  |
|  | $(1.59)$ | $(1.65)$ | $(1.58)$ | $(0.15)$ | $(0.15)$ | $(0.06)$ |  |  |  |  |  |
| (True) Logit route $\sigma^{R}$ | 0.43 | 0.53 | 0.20 | 0.05 | -0.05 | $1.03^{* * *}$ |  |  |  |  |  |
| Observations | $(0.57)$ | $(0.53)$ | $(0.46)$ | $(0.06)$ | $(0.04)$ | $(0.02)$ |  |  |  |  |  |

Notes: This table uses simulated data of exactly the same size as the data used in estimation to describe the finite sample properties of the estimation procedure. See notes for Figure A4 Each column reports results from a quantile (median) regression of the estimated parameter on the vector of true parameters. ${ }^{*} p \leq 0.10$, ${ }^{* *} p \leq 0.05,{ }^{* * *} p \leq 0.01$


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    Supplementary Materials available at/sites.google.com/site/gabrielkreindler/cp-sm
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[^1]:    ${ }^{1}$ The congestion charge policy in Stockholm and Singapore's Electronic Road Pricing (ERP) policy have higher fees during the morning and evening peak hours. Jakarta's former "3-in-1" and the current "odd-even" policies are in effect during morning and evening peak hours only. Similarly, Manila's Unified Vehicular Volume Reduction Program (UVVRP) only applies during peak hours in certain parts of the city.

[^2]:    ${ }^{2}|x|_{-}$and $|x|_{+}$denote the negative and positive parts of $x$.

[^3]:    ${ }^{3}$ In an independent randomization not analyzed here, the congestion charge was $50 \%$ higher on two randomly chosen days.

[^4]:    ${ }^{4}$ There is an increase in trips around half an hour after the end of the congestion charge. The exact position of this increase does not map cleanly to the predicted response given marginal incentives, as in the case of the early morning. This increase is entirely concentrated among non-commuting trips; Figure A1 shows that this effect disappears for commuting trips of regular commuters. Instead, there is a slight substitution to later times during the decreasing "ramp." This result suggests the possibility of discrete scheduling changes for some non-commuting trips.

[^5]:    ${ }^{5}$ The results are broadly similar when using total daily hy charges (equal to the hypothetical rate multiplied by the trip length) or when using trips as observations, with stronger effects in the morning than in the evening.

[^6]:    ${ }^{6}$ While not directly targeted as a moment, for each commuter, I also use the smoothed distribution of departure times before the experiment to invert the ideal departure time distribution (section 7.3 .

[^7]:    ${ }^{7}$ For computational reasons, I only use one random starting condition for GMM estimation. This is a likely reason for a very small number of cases where the estimated parameter is slightly different from the true value.
    ${ }^{8}$ In theory, the identification of the discount factor leverages the variation in future expected utility, but not current

[^8]:    ${ }^{10}$ I cannot separate the impact of motorcycles and cars, and cannot account for vehicle occupancy. In the study sample, the share of trips made by car is roughly constant throughout the day, at around a third. My results should be interpreted as the average effect along these dimensions. In the GPS data, cars are $2.5 \%$ faster outside peak-hours, and have the same speed during peak-hours.

[^9]:    ${ }^{11}$ This calculation is independent of the number of trips in the sample. Intuitively, this is because equation 8 depends on density divided by the number of trips. See Appendix A. 6 for the full proof.
    ${ }^{12}$ The $R^{2}$ of the regression of trip departure time in the morning on morning recruiting time is below 0.05 , and below 0.02 for the evening (Figure A5 panel C).

[^10]:    ${ }^{13}$ I thank an anonymous referee for this point.
    ${ }^{14}$ I made these queries in 2021. Despite overall lower traffic levels due to Covid 19, trip-level travel time and travel delay at 9 am correlate strongly with 2017 data ( $R^{2}=0.93$ and $R^{2}=0.5$ ).
    ${ }^{15}$ However, note that the slope in Bangalore is several times shallower than the slope identified based on taxi trips in Geroliminis and Daganzo (2008) in Yokohama, Japan.

[^11]:    ${ }^{16}$ As a back of the envelope calculation, census data shows that in 2011 roughly the same fraction of workers used buses as private vehicles in Bangalore. Assuming a value of time twice as small for bus users, and assuming a similar distribution of departure times and distances, the 2.5 minute improvement in average travel time for bus users is worth approximately 13.9 INR on average per driver, i.e. $31 \%$ more than welfare gains among drivers.
    ${ }^{17}$ In my model, higher inflexibility makes it more difficult to induce drivers to change their departure times. This leads to departure times that are dictated more by ideal arrival times rather than travel time savings of leaving earlier or later. Overall, this limits the gains from optimal pricing. Equilibrium feedback forces are stronger in Arnott et al. 1993 because commuters as homogeneous. The slope of the travel time profile is $\beta_{E} / \alpha$ and $\beta_{L} / \alpha$ before and after the peak, and the deadweight loss of congestion (in levels) is increasing in schedule costs.

[^12]:    ${ }^{18}$ In the classic Pigou-Knight model travel times on the two routes are equalized in equilibrium. Here, this is not the case because of nested logit preferences. Simulating the model with $\sigma^{R}$ four times smaller yields similar results. The two route have similar usage primarily because of sufficiently similar externalities, not because of idiosyncratic route preferences.
    ${ }^{19}$ The congestion pricing experiment was not designed to estimate the extensive margin trip elasticity, because of the concern that commuters would game incentives by not taking their smartphones with them when traveling, and because this margin plausibly requires more time (see Martin and Thornton (2017) for extensive margin results over several months).

[^13]:    ${ }^{20}$ The quadratic shape implies unrealistic negative travel time for very early or very late departure time. I later assume that schedule costs rise faster so that, on net, these departure times are unattractive.

